Digital VLSI Design

Lecture 8: Clock Tree Synthesis

Semester A, 2018-19

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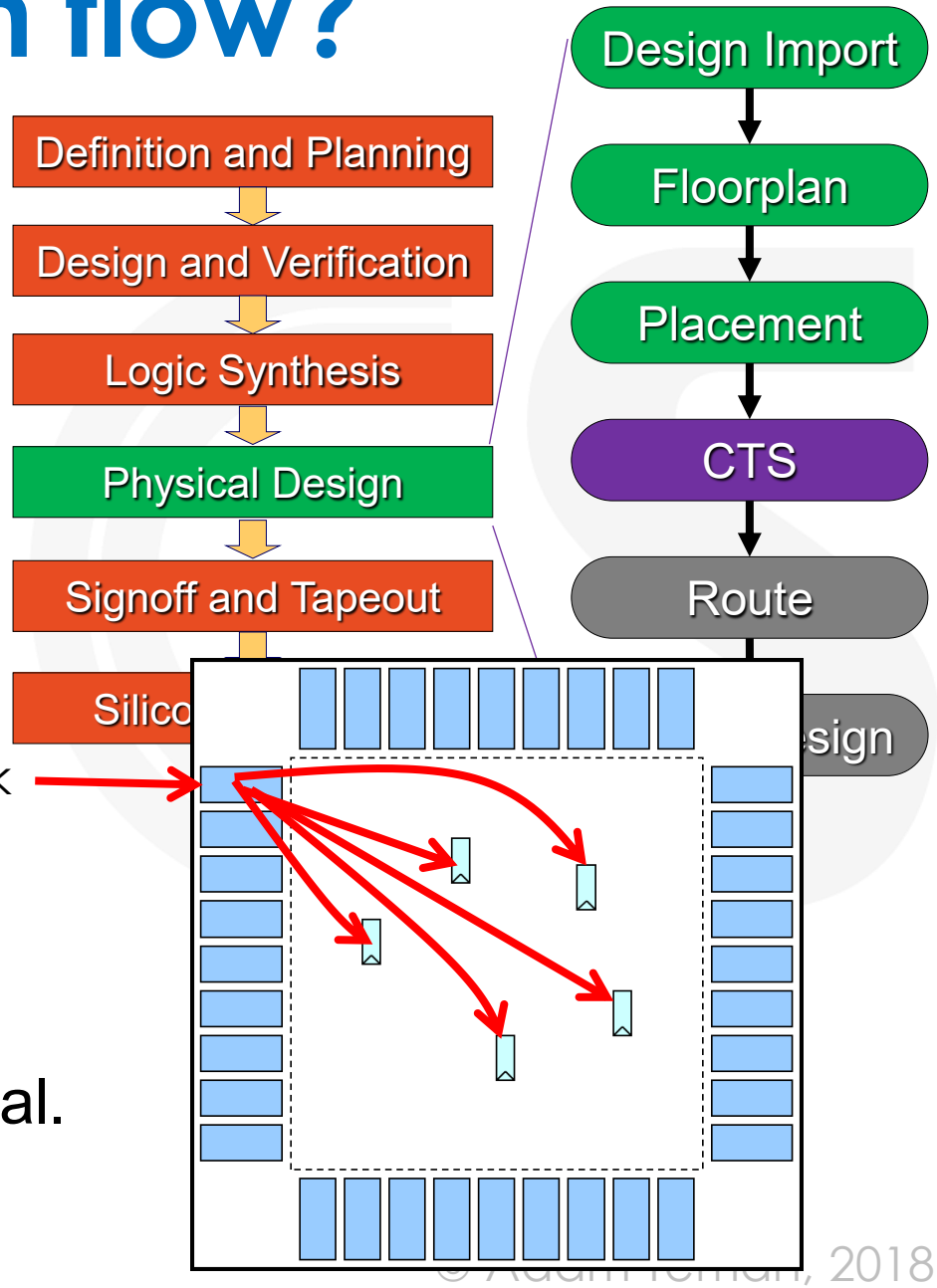
Emerging Nanoscaled Integrated Circuits and Systems Labs

Bar-Ilan University
אוניברסיטת בר-אילן

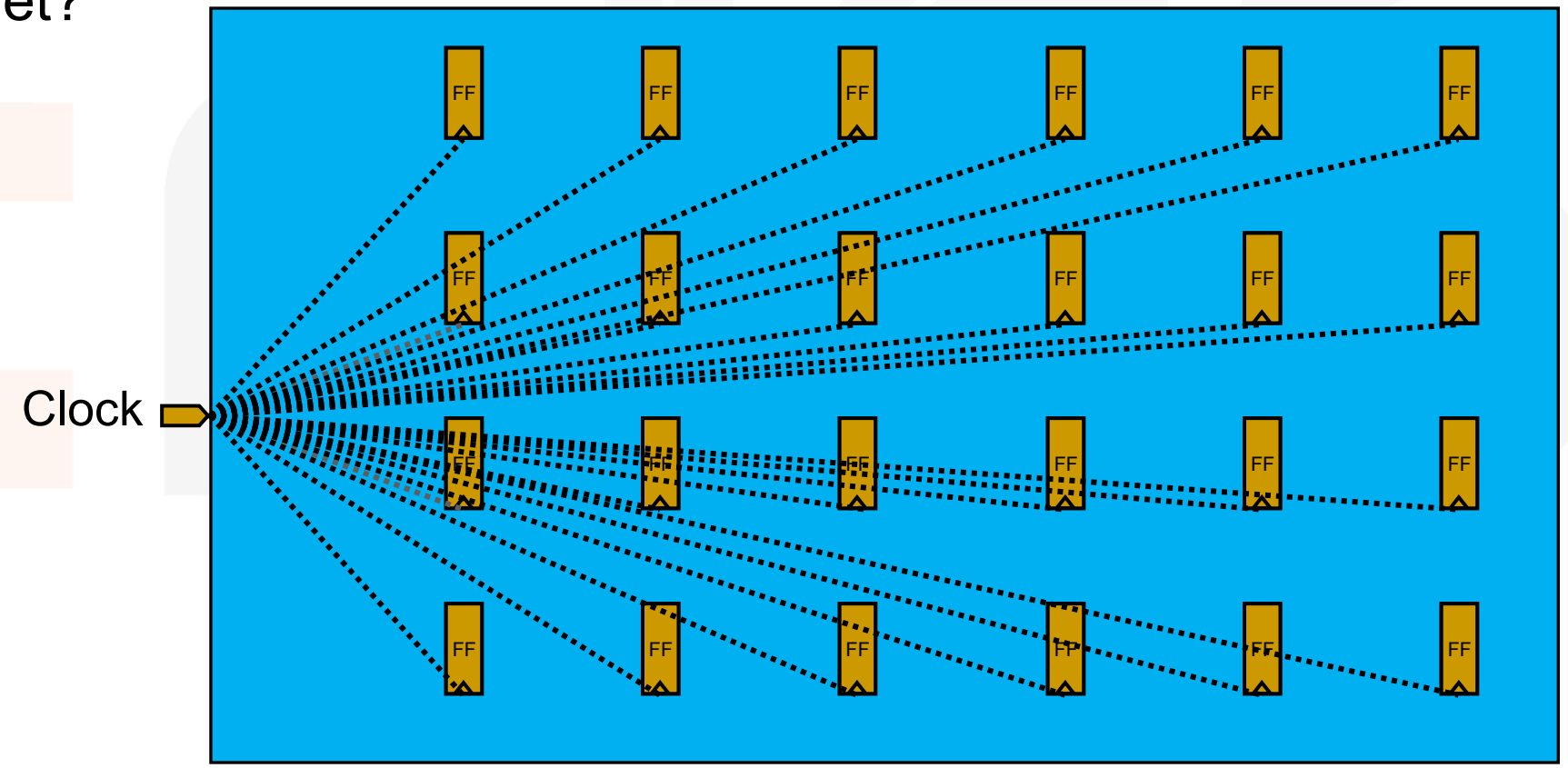
Where are we in the design flow?

- **We have:**
  - Synthesized our design into a technology mapped gatelevel netlist
  - Designed a floorplan for physical implementation.
  - And provided a location for each and every gate.
- **During all stages:**
  - We analyzed timing constraints and optimized the design according to these constraints.
- **However…**
  - Until now, we have assumed an ideal clock.
  - Now we have <u>all sequential elements placed</u>, so we have to provide them with a ***real*** clock signal.

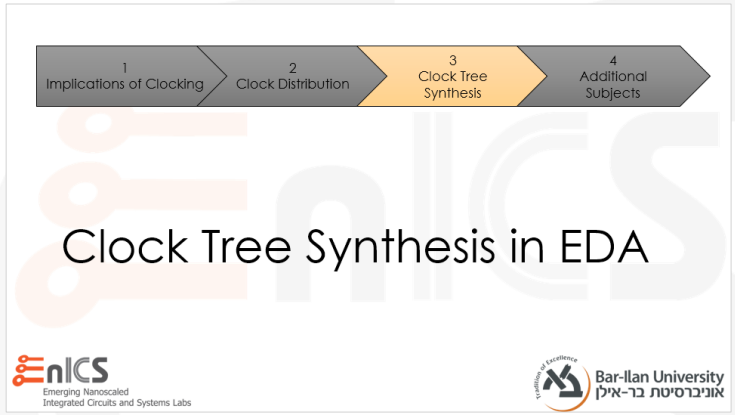


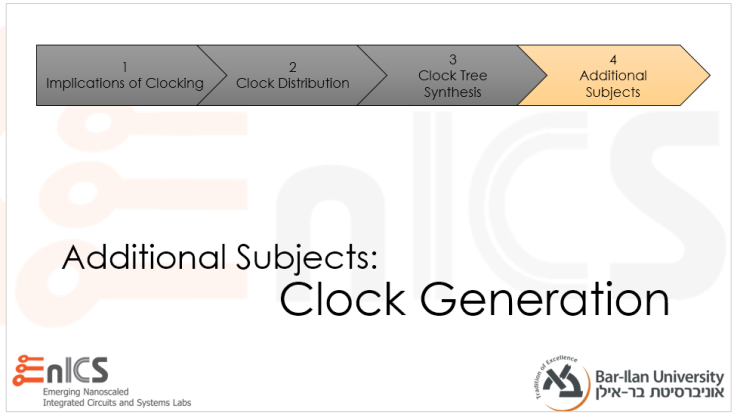
Trivial Approach?

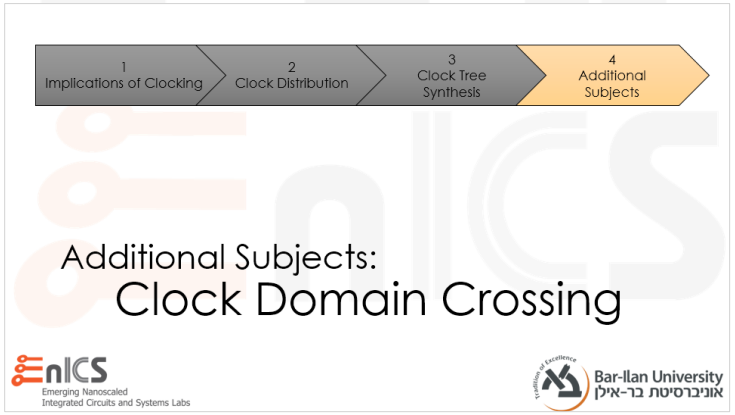
- **Question:**
  - Why not just route the clock net to all sequential elements, just like any other net?
- **Answer…**
  - Timing
  - Power
  - Area
  - Signal Integrity
  - etc…



Lecture Outline





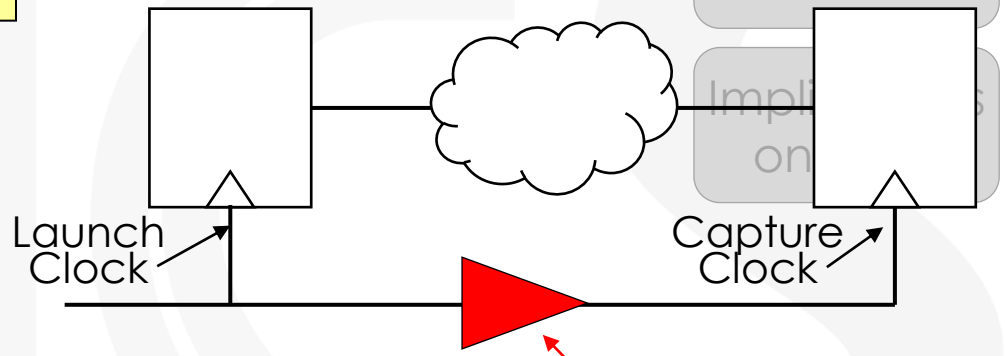


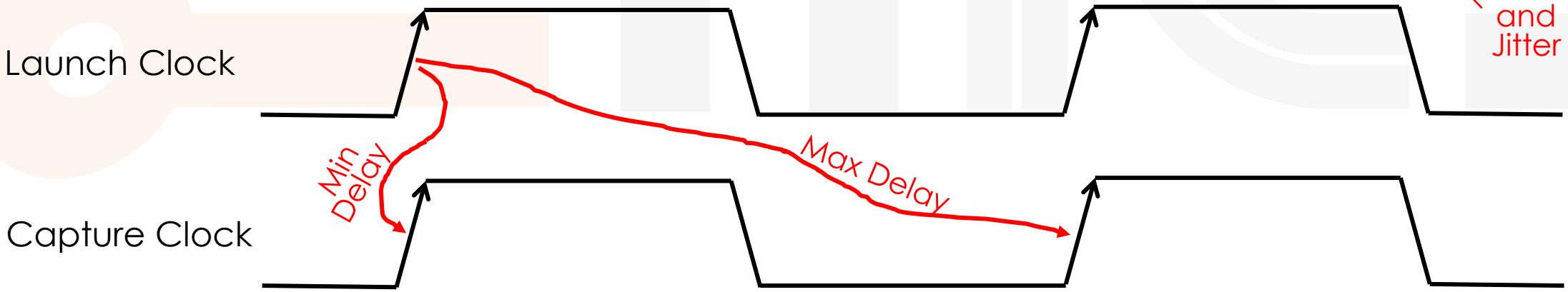
Implications of Clocking

Timing, power, area, signal integrity

Implications on Timing

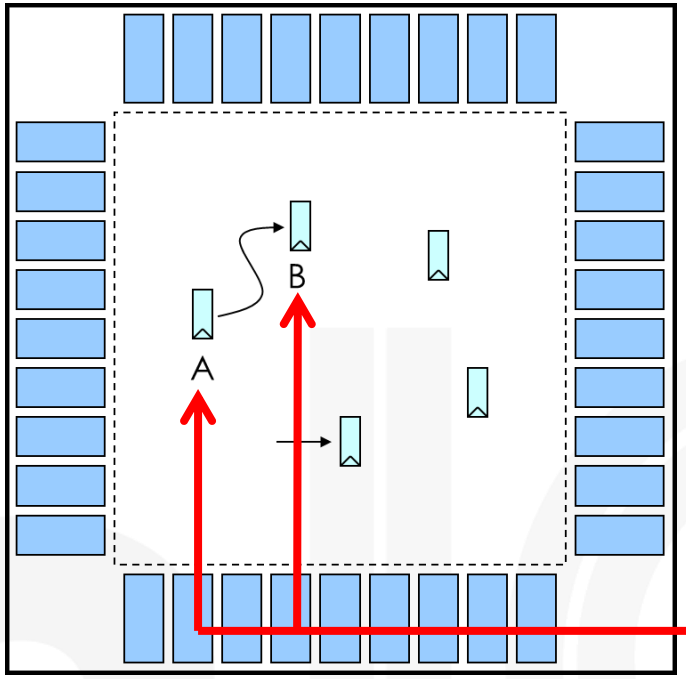
- **Let's remember our famous timing constraints:**
  - Max Delay: $T + \delta_{skew} > t_{CQ} + t_{logic} + t_{setup} + \delta_{margin}$
  - Min Delay: $t_{CQ} + t_{logic} - \delta_{margin} > t_{hold} + \delta_{skew}$

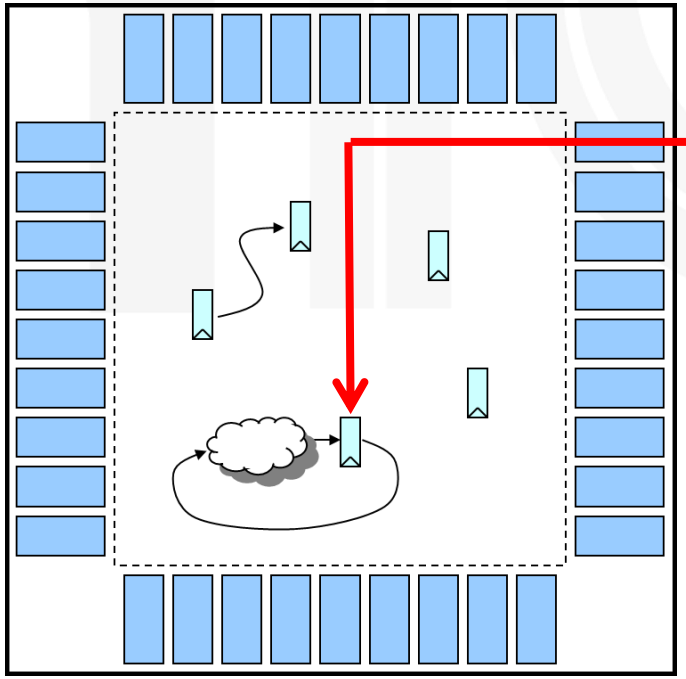




Clock Parameters

- **Skew**
  - Difference in clock arrival time at two different registers.
- **Jitter**
  - Difference in clock period between different cycles.
- **Slew**
  - Transition (t_{rise}/t_{fall}) of clock signal.
- **Insertion Delay**
  - Delay from clock source until registers.



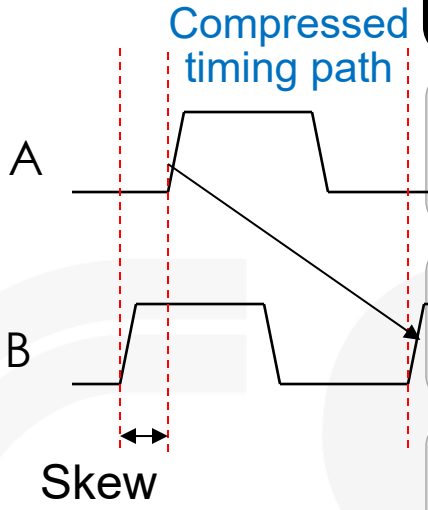


Implications on Timing

Implications on Power

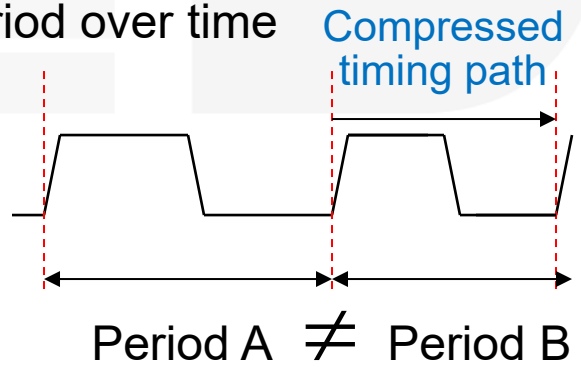
Implications on SI

Implications on Area



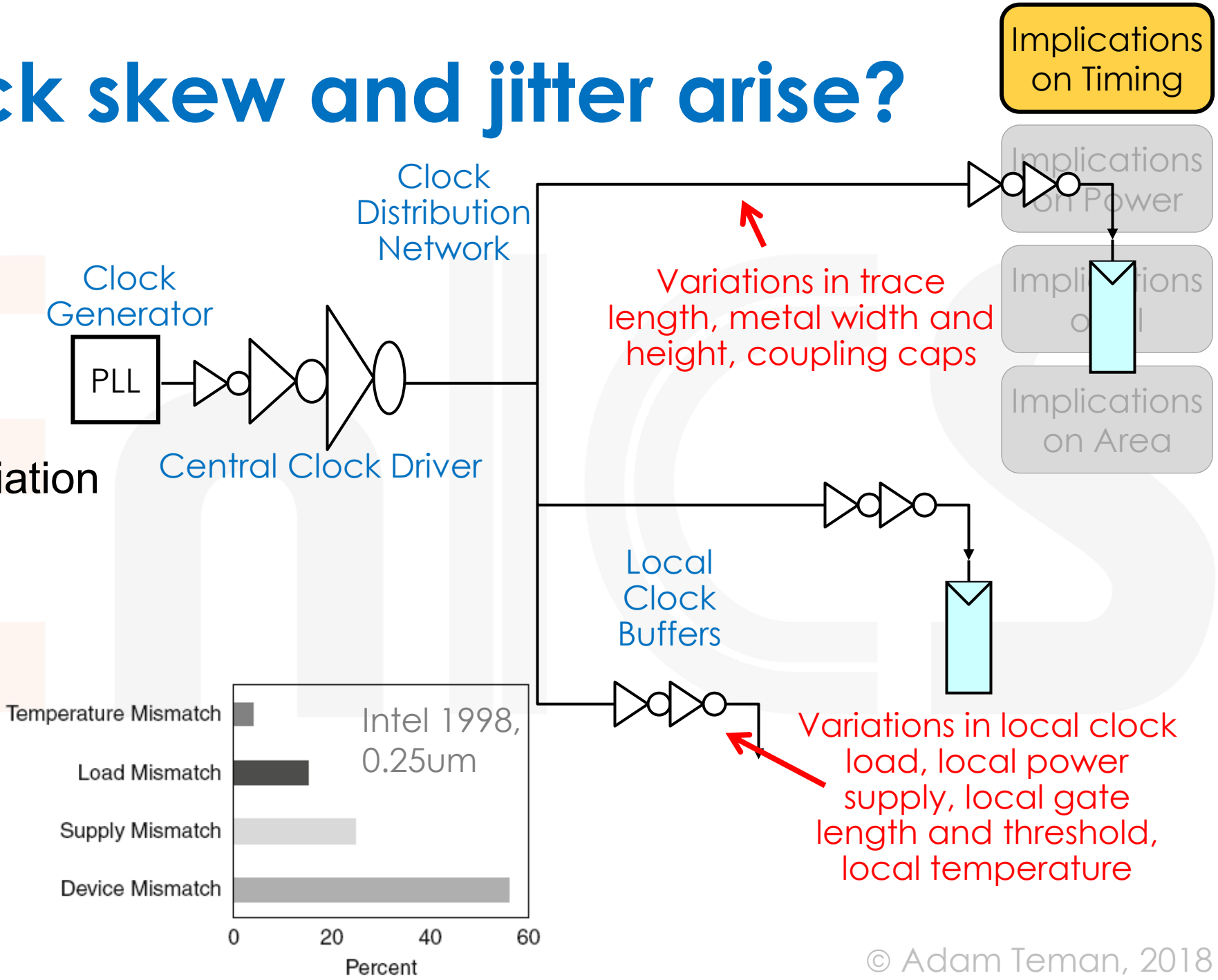
Clock Skew
Difference in clock arrival time at two spatially distinct points

Clock Jitter
Difference in clock period over time



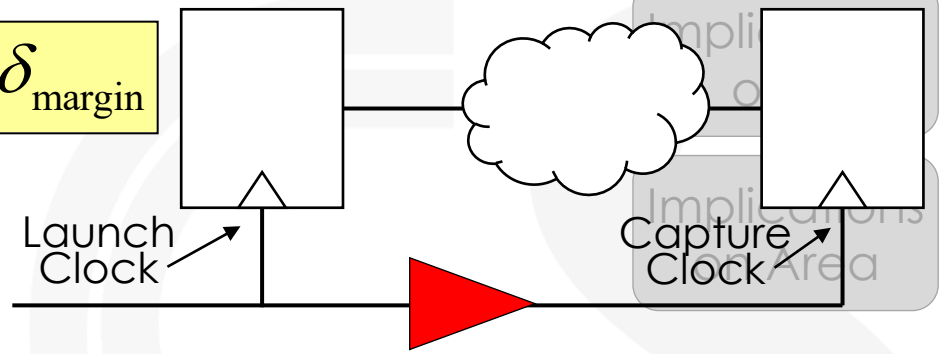
How do clock skew and jitter arise?

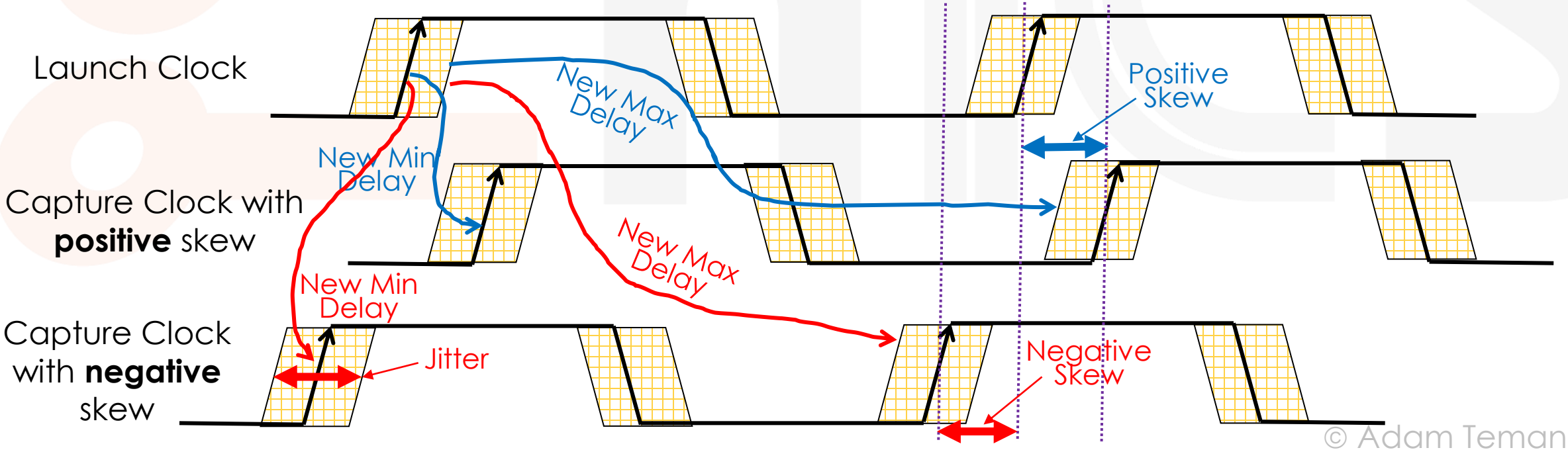
- **Clock Generation**
- **Distribution network**
  - Number of buffers
  - Device Variation
  - Wire length and variation
  - Coupling
  - Load
- **Environment Variation**
  - Temperature
  - Power Supply



Implications on Timing

- **So skew and jitter eat away at our timing margins:**
  - Max Delay: $T + \delta_{skew} - 2\delta_{jitter} > t_{CQ} + t_{logic} + t_{setup} + \delta_{margin}$
  - Min Delay: $t_{CQ} + t_{logic} - \delta_{margin} > t_{hold} + \delta_{skew}$



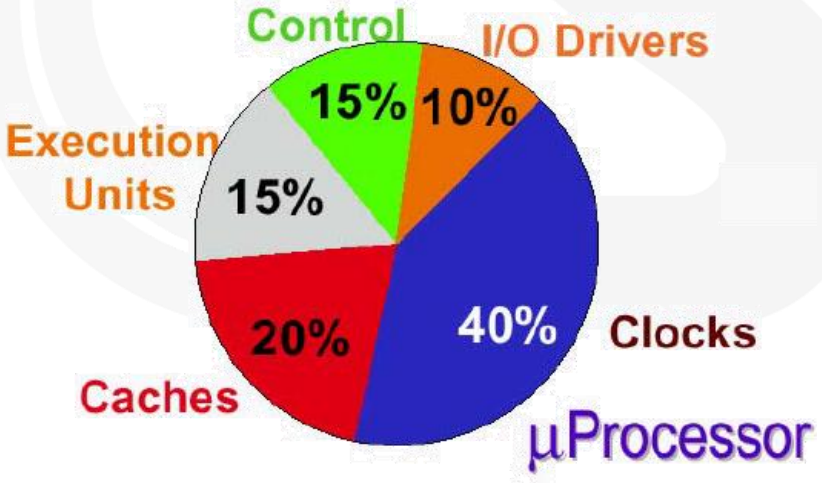


Implications on Power

- **Let's remember how to calculate dynamic power:**

$$P_{\text{dyn}} = f \cdot C_{\text{eff}} \cdot V_{\text{DD}}^2 \qquad C_{\text{eff}} \triangleq \alpha \cdot C_{\text{total}} = \alpha_{\text{clock}} \cdot C_{\text{clock}} + \alpha_{\text{others}} \cdot C_{\text{others}}$$

  - The activity factor (α) of the clock network is 100%!
- **The clock capacitance consists of:**
  - Clock generation (i.e., PLL, clock dividers, etc.)
  - Clock elements (buffers, muxes, clock gates)
  - Clock wires
  - Clock load of sequential elements
- **Clock networks are huge**
  - And therefore, the clock is responsible for a large percentage of the total chip power.



Possible power partitioning of a microprocessor (*not general!!!*)

Implications on Signal Integrity

Signal Integrity is an obvious requirement for the clock network:

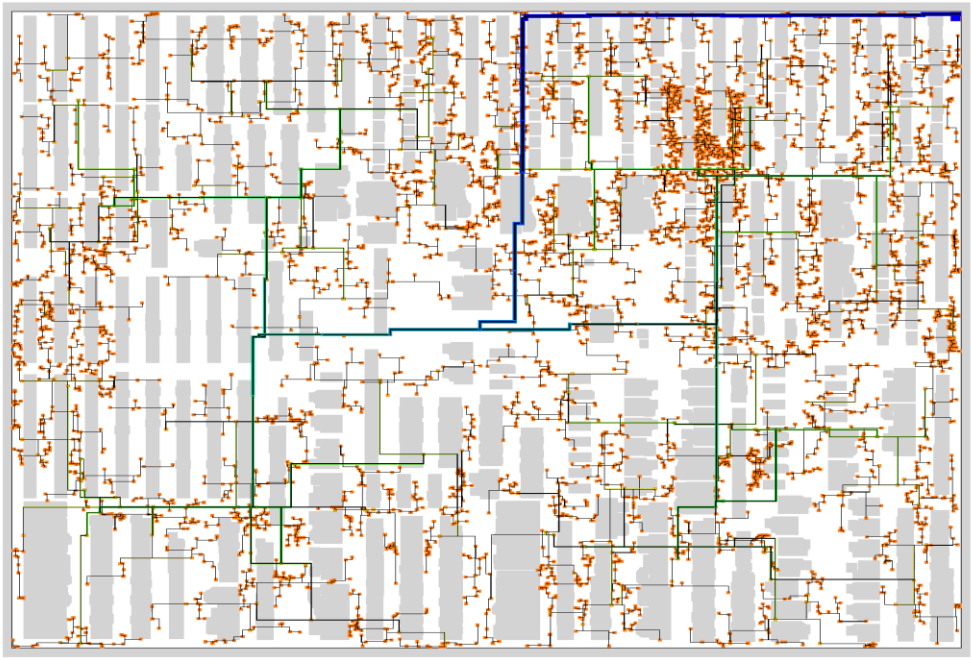
- **Noise on the clock network can cause:**
  - In the worst case, additional clock edges
  - Lower coupling can still slow down or speed up clock propagation
  - Irregular clock edges can impede register operation
- **Slow clock transitions (slew rate):**
  - Susceptibility to noise (weak driver)
  - Poor register functionality (worse t_{cq}, t_{setup}, t_{hold})
- **Too fast clock transitions**
  - Overdesign → power, area, etc.
  - Bigger aggressor to other signals
- **Unbalanced drivers lead to increased skew.**

Best practice:
Keep t_{rise} and t_{fall} between 10-20% of clock period (e.g., 100-200ps @1GHz)

Implications on Area

- **To reiterate, clock networks consist of:**
  - Clock generators
  - Clock elements
  - Clock wires
- **All of these consume area**
  - Clock generators (e.g., PLL) can be very large
  - Clock buffers are distributed all over the place
  - Clock wires consume a lot of routing resources
- **Routing resources are most vital**
  - Require low RC (for transition and power)
    - Benefit of using high, wide metals
  - Need to connect to every clock element (FF)
    - Distribution all over the chip
    - Need Via stack to go down from high metals

For example: **Intel Itanium**
4% of M4/M5 used for clock routing



Source: Universitat Bonn

Clock Distribution

So how do we build a clock tree?

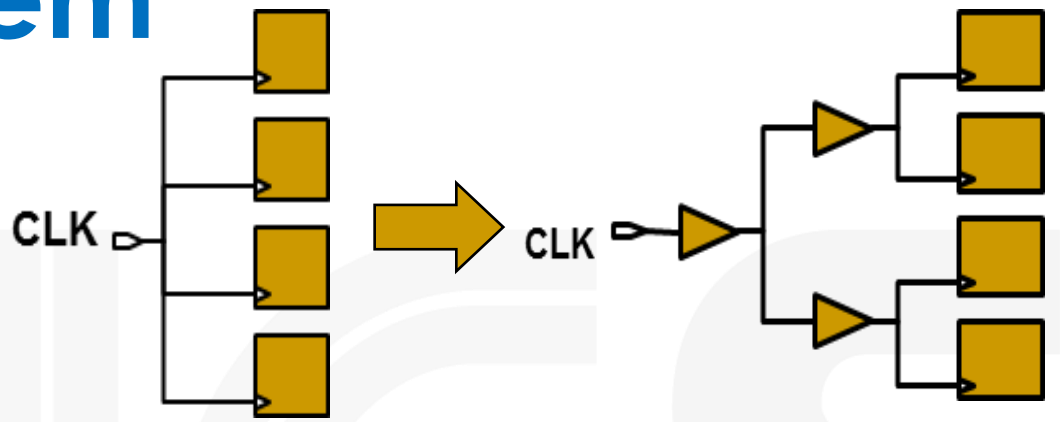
The Clock Routing Problem

Given a source and *n* sinks:

- **Connect all sinks to the source by an interconnect network so as to minimize:**
  - Clock Skew = $\max_{i,j} |t_i - t_j|$
  - Delay = $\max_i (t_i)$
  - Total wirelength
  - Noise and coupling effect

The Challenge:

- **Synchronize millions (billions) of separate elements**
  - Within a time scale on order of ~ 10 ps
  - At distances spanning 2-4 cm
    - Ratio of synchronizing distance to element size on order of 10^5
  - Reference: light travels <1 cm in 10 ps

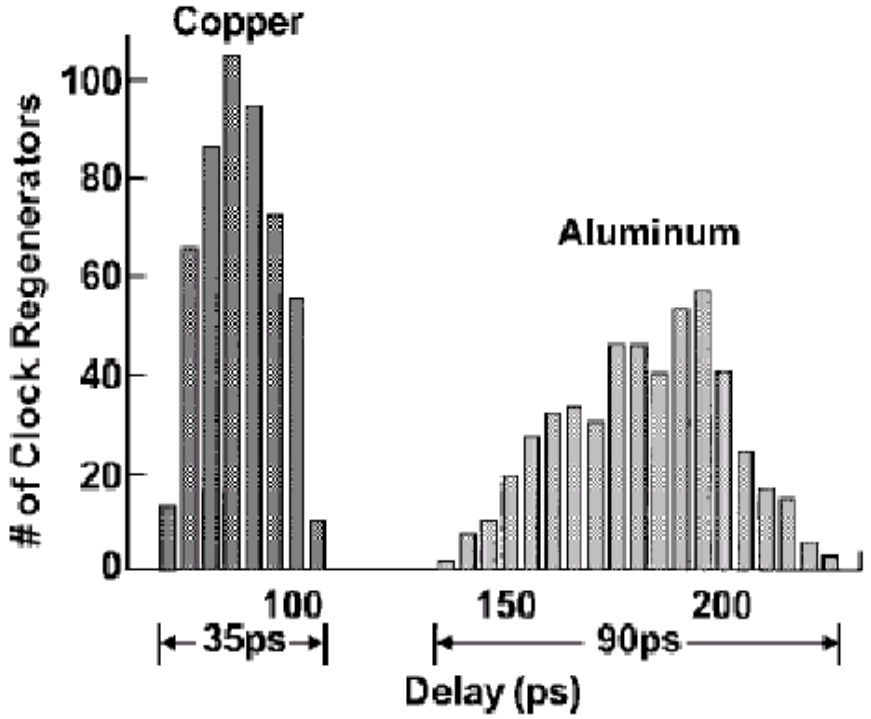


Clock Tree goals:
1) Minimize Skew
2) Meet target insertion delay (min/max)

Clock Tree constraints:
1) Maximum Transition
2) Maximum load cap
3) Maximum Fanout
4) Maximum Buffer Levels

Technology Trends

- **Timing**
  - Higher clock frequency → Lower skew
  - Higher clock frequency → Faster transitions
  - Jitter – PLL's get better with CMOS scaling
  - but other sources of noise increase
    - Power supply noise more important
    - Switching-dependent temperature gradients



- **New Interconnect Materials**
  - Copper Interconnect → Lower RC → Better slew and potential skew
  - Low-k dielectrics → Lower clock power, better latency/skew/slew rates
- **Power**
  - Heavily pipelined design → more registers → more capacitive load for clock
  - Larger chips → more wire-length needed to cover the entire die
  - Complexity → more functionality and devices → more clocked elements
  - Dynamic logic → more clocked elements

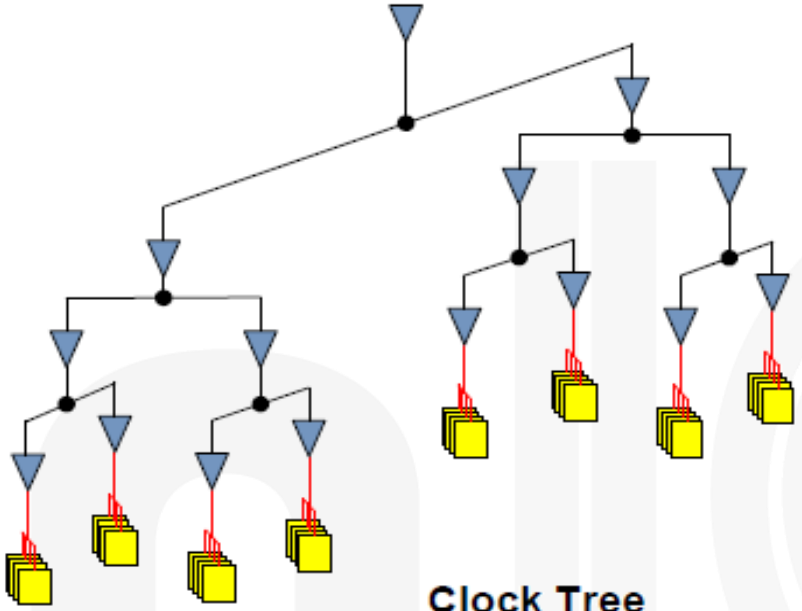
Approaches to Clock Synthesis

Clock Tree

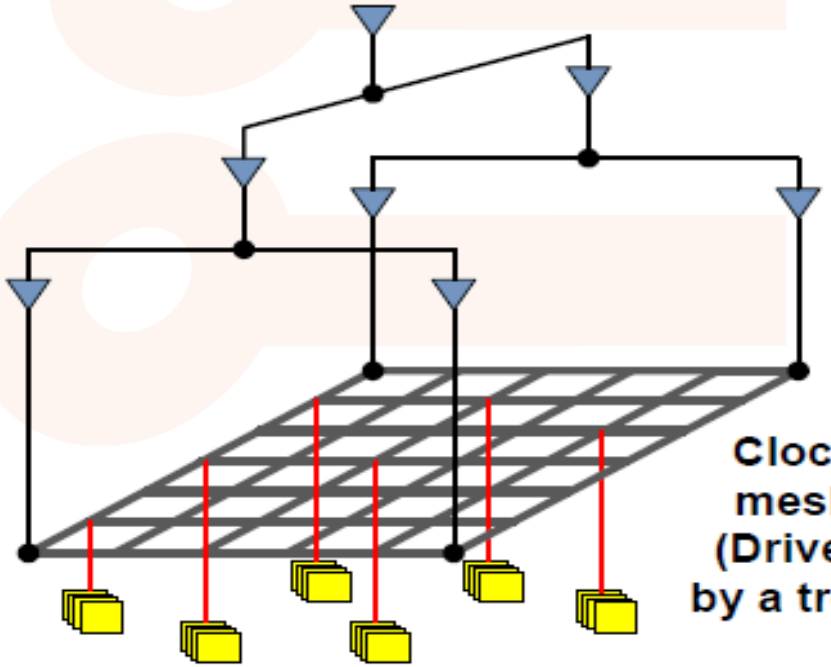
Clock Grid

Clock Spine

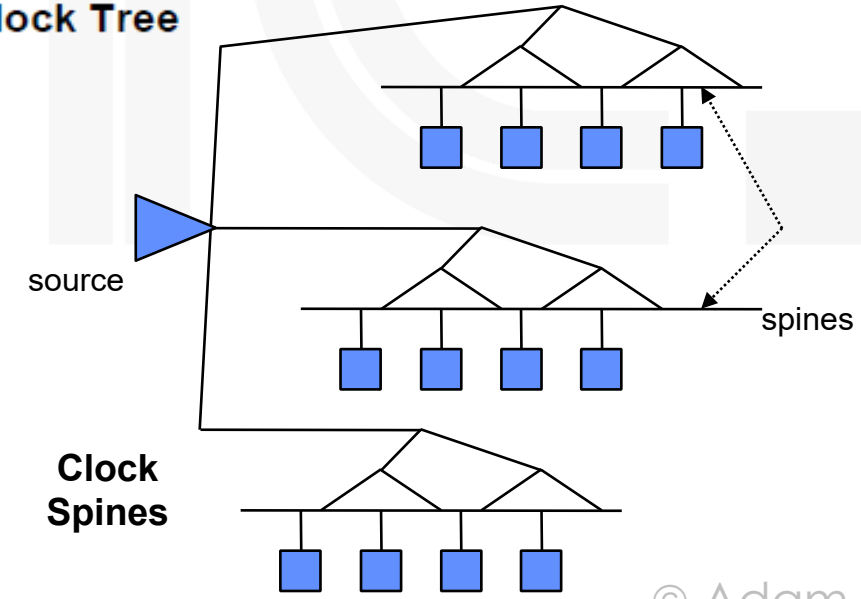
- **Broad Classification:**
  - Clock Tree
  - Clock Mesh (Grid)
  - Clock Spines



Clock Tree



Clock mesh (Driven by a tree)



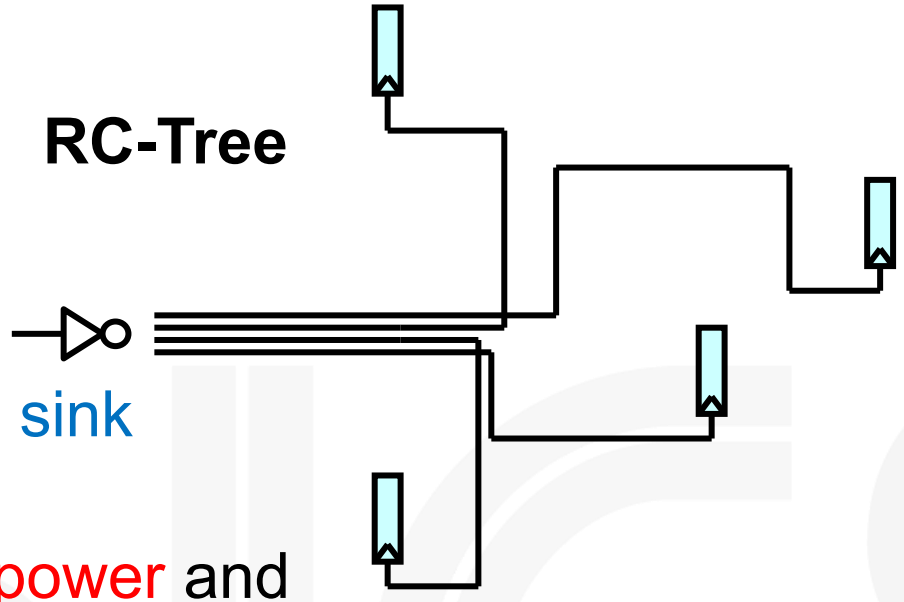
Clock Spines

Clock Trees

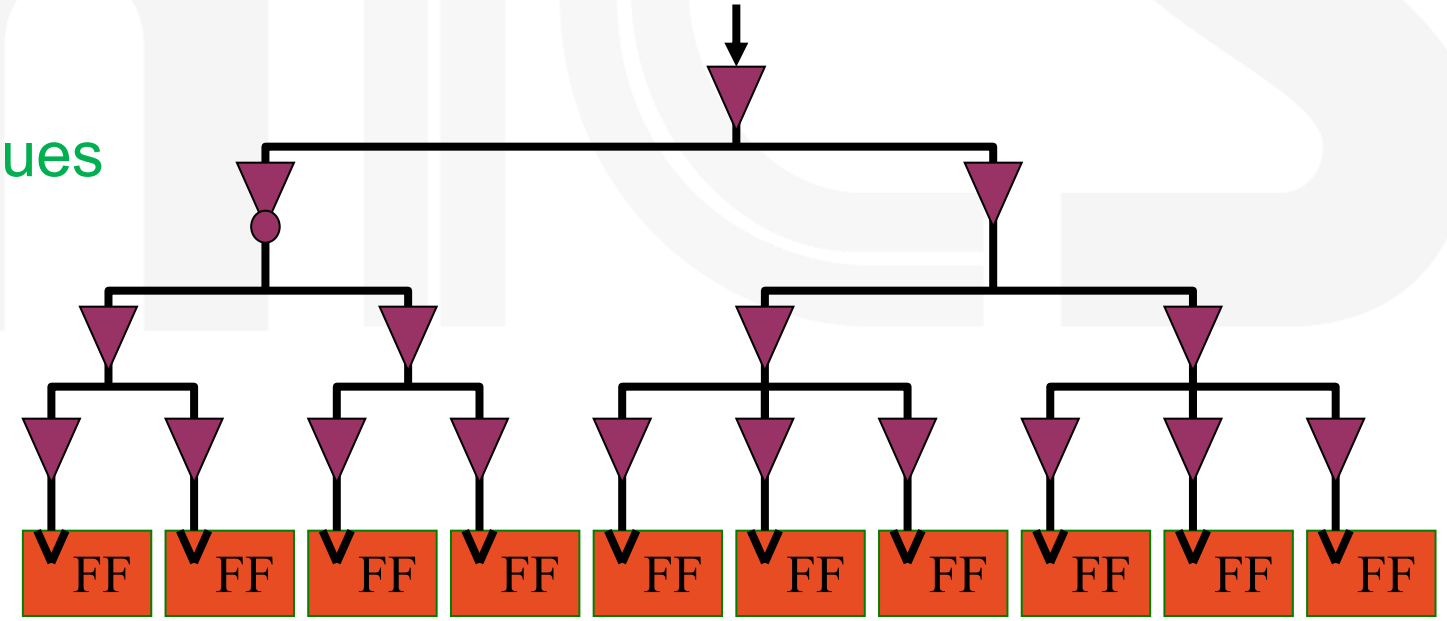
Clock Tree

Clock Grid

Clock Spine



- **Naïve approach:**
  - Route an individual clock net to each sink and balance the RC-delay
  - However, this would burn excessive power and the large RC of each net would cause signal integrity issues.
- **Instead use a buffered tree**
  - Short nets mean lower RC values
  - Buffers restore the signal for better slew rates
  - Lower total insertion delay
  - Less total switching capacitance



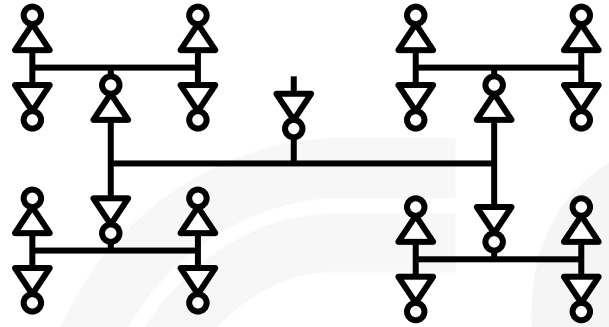
Building an actual Clock Tree

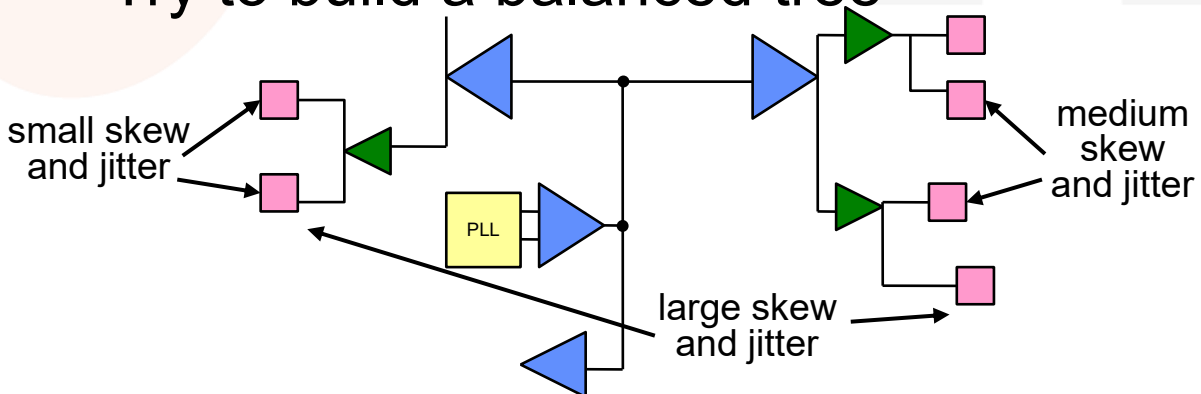
Clock Tree

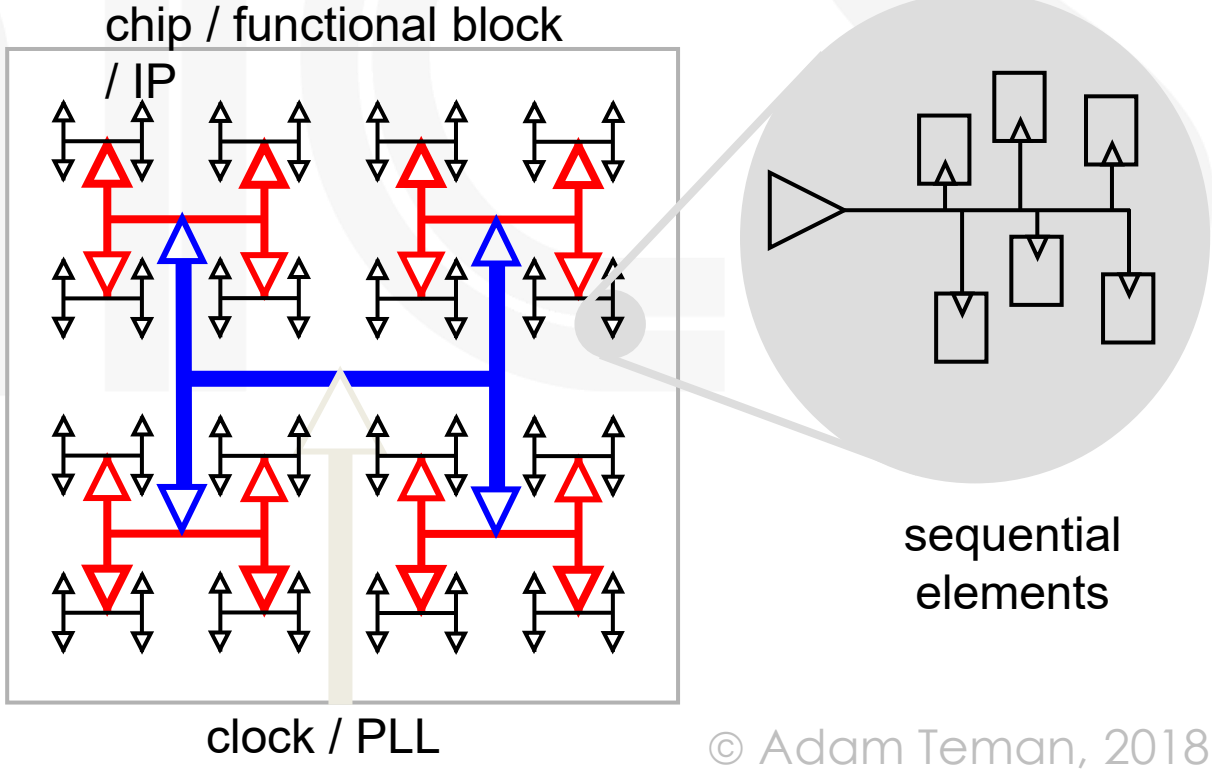
Clock Grid

Clock Spine

- **Perfectly balanced approach: H-Tree**
  - One large central driver
  - Recursive H-style structure to match wire-lengths
  - Halve wire width at branching points to reduce reflections
- **More realistic:**
  - Tapered H-Tree, but still hard to do.
- **Standard CTS approach:**
  - Flip flops aren't distributed evenly.
  - Try to build a balanced tree







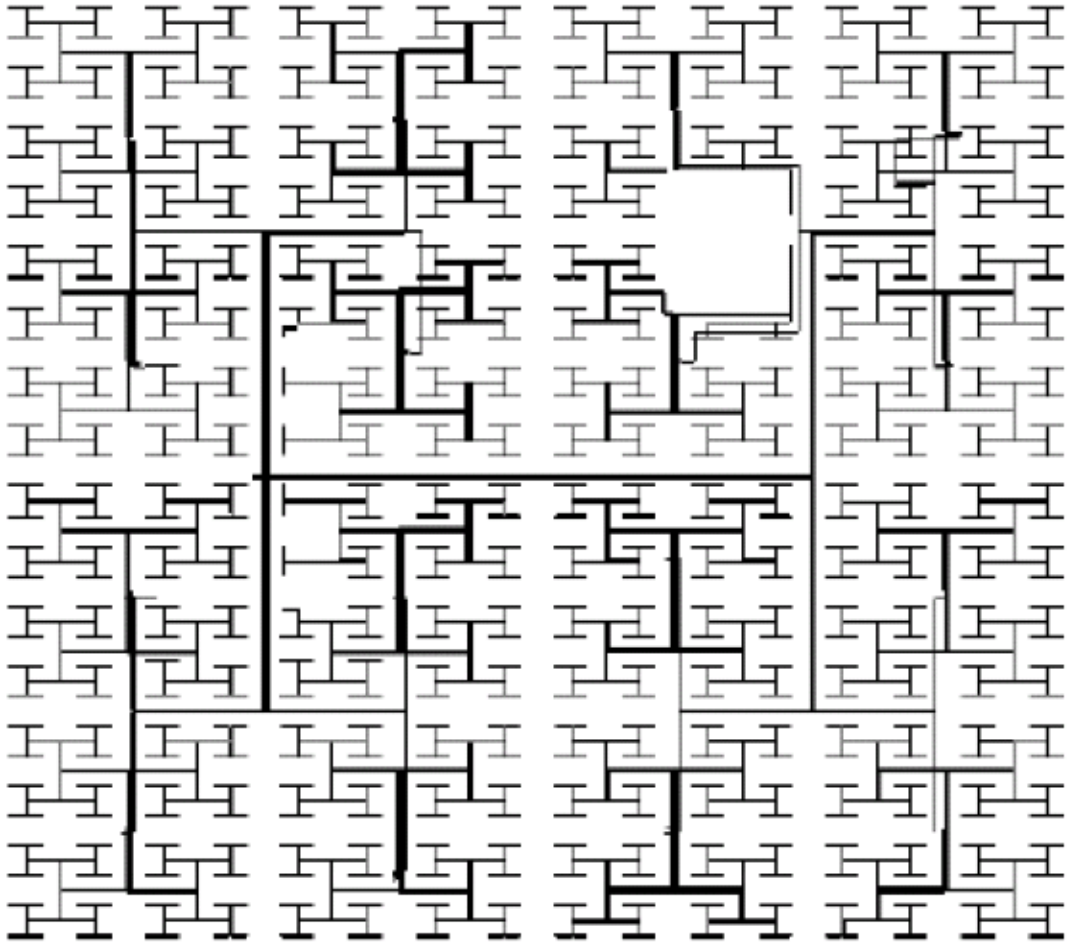
Industrial H-Tree Examples

Clock Tree

Clock Grid

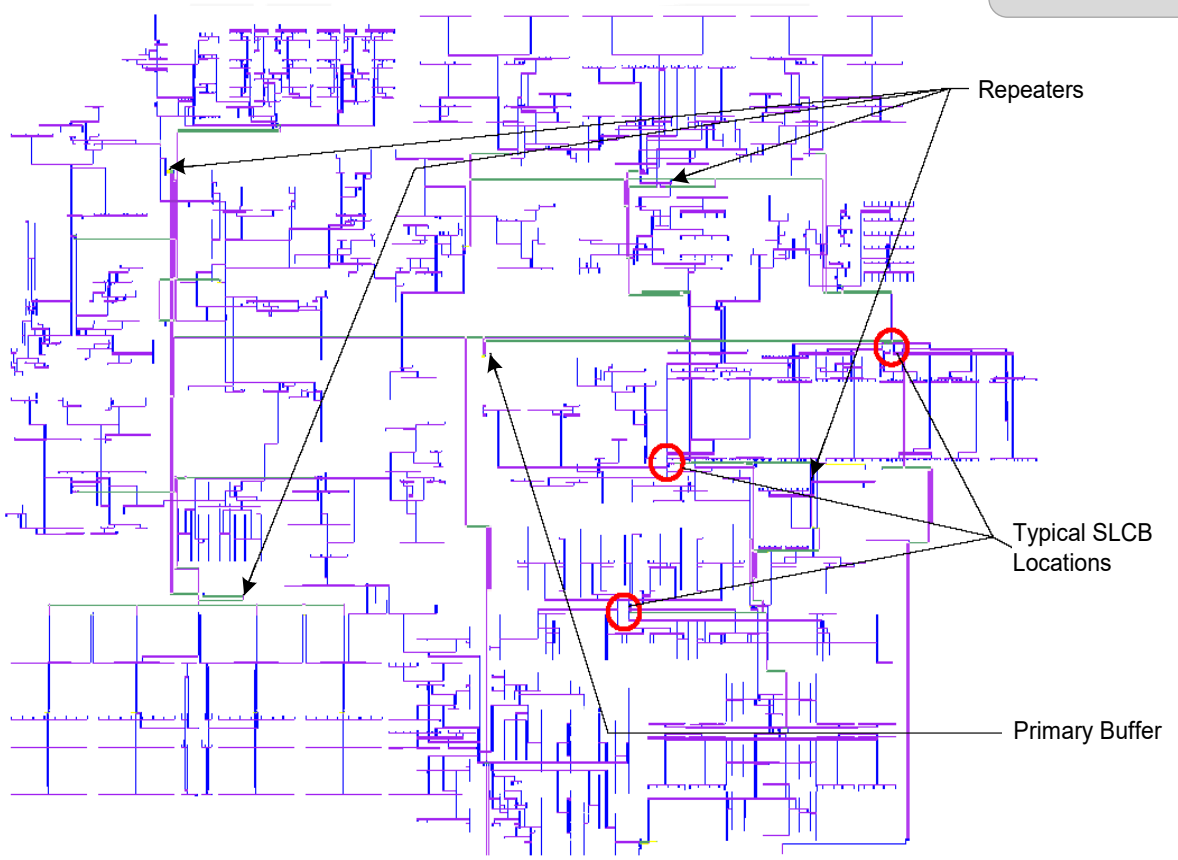
Clock Spine

- IBM PowerPC (2002)



IBM, ISSCC 2000

- Intel Itanium 2 (2005)



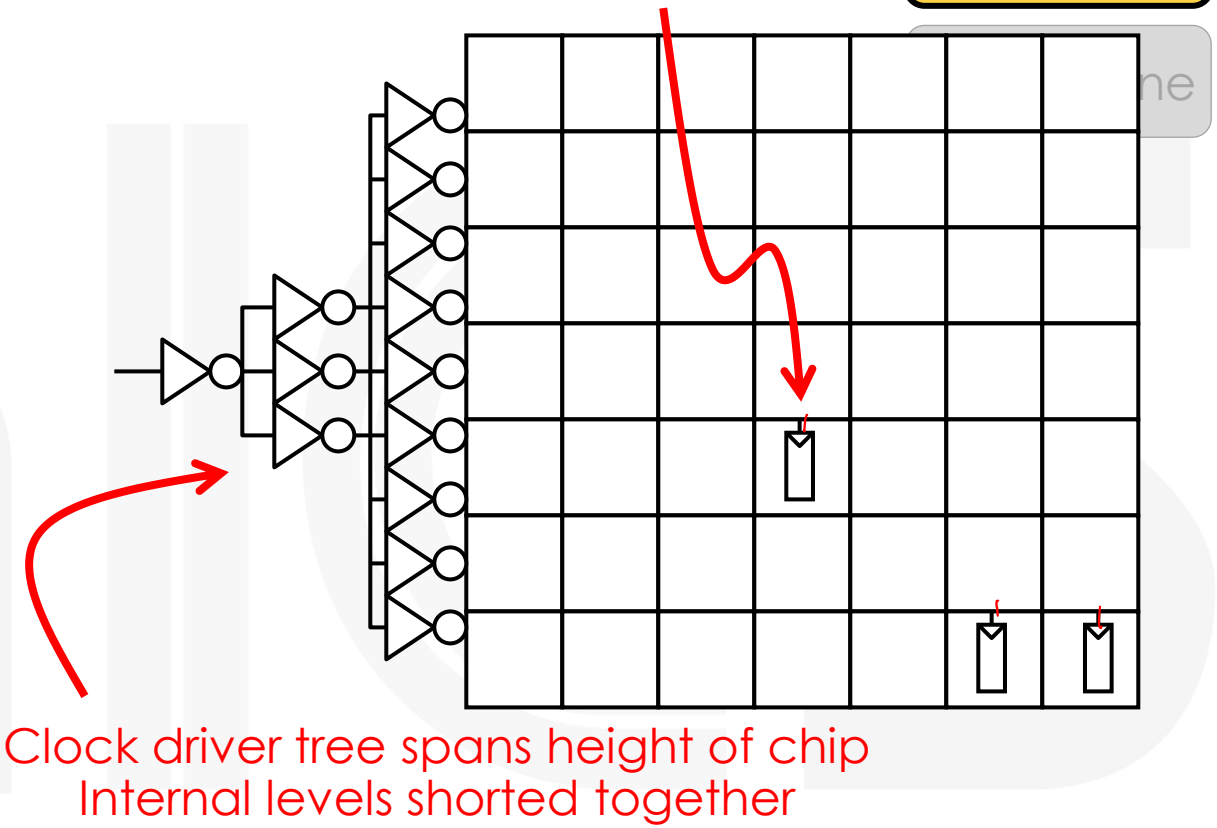
Source: CMOS VLSI Design, 4th Ed.

Lower Skew – Clock Grids

Clock Tree

Clock Grid

- **Advantages:**
  - Skew determined by grid density and not overly sensitive to load position
  - Clock signals are available everywhere
  - Tolerant to process variations
  - Usually yields extremely low skew values
- **Disadvantages**
  - Huge amounts of wiring & power
    - Wire cap large
    - Strong drivers needed – pre-driver cap large
    - Routing area large
  - To minimize all these penalties, make grid pitch coarser
    - Skew gets worse
    - Losing the main advantage
  - Don't overdesign – let the skew be as large as tolerable
  - Still – grids seem non-feasible for SoC's



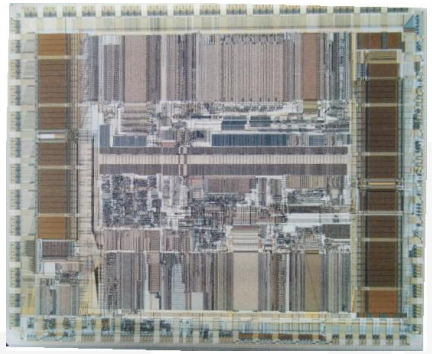
DEC Alpha – Generations of Grids

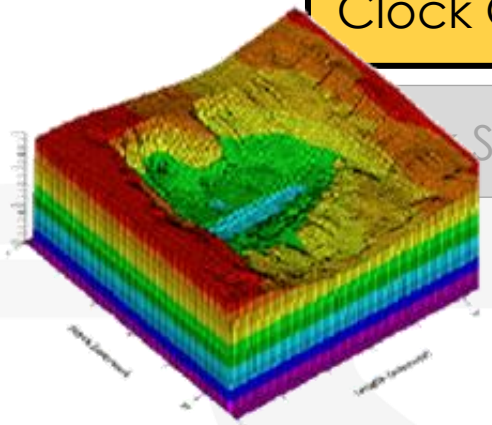
Clock Tree

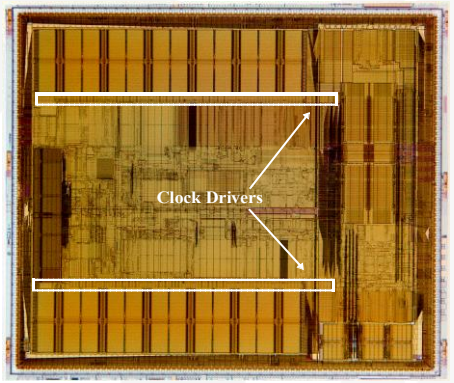
Clock Grid

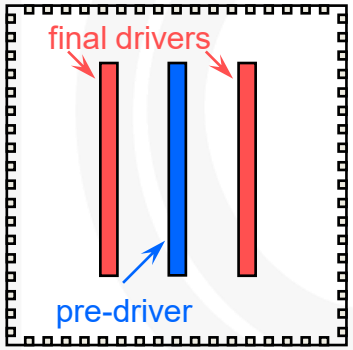
Spine

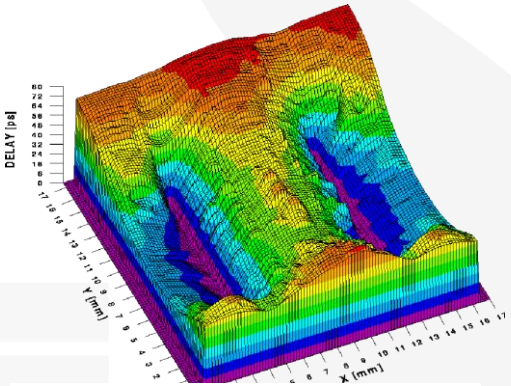
- **21064 (EV4) – 1992**
  - 0.75µm, 200MHz, 1.7M trans.
  - Big central driver, clock grid
    - 240ps skew
- **21164 (EV5) - 1995**
  - 0.5 µm, 300MHz, 9.3M trans.
  - Central driver, two final drivers, clock grid
    - Total driver size – 58 cm!
    - 120ps skew
- **21264 (EV6) - 1998**
  - 0.35 µm, 600MHz, 15.2M trans.
  - 4 skew areas for gating
    - Total driver size: 40 cm
    - 75ps skew

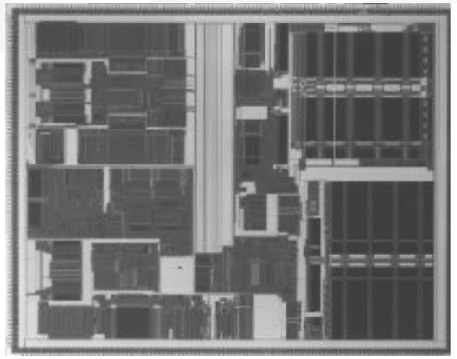


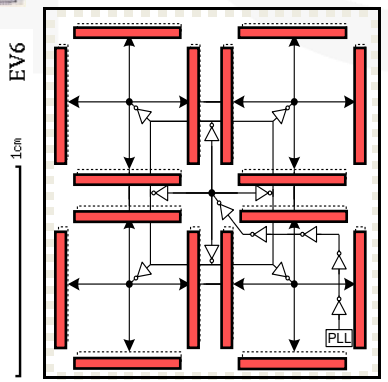


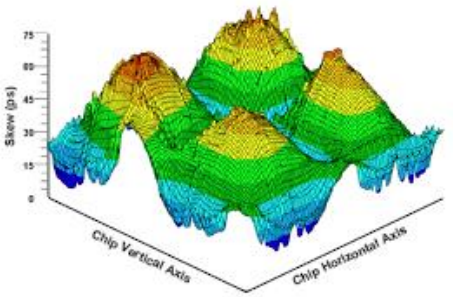






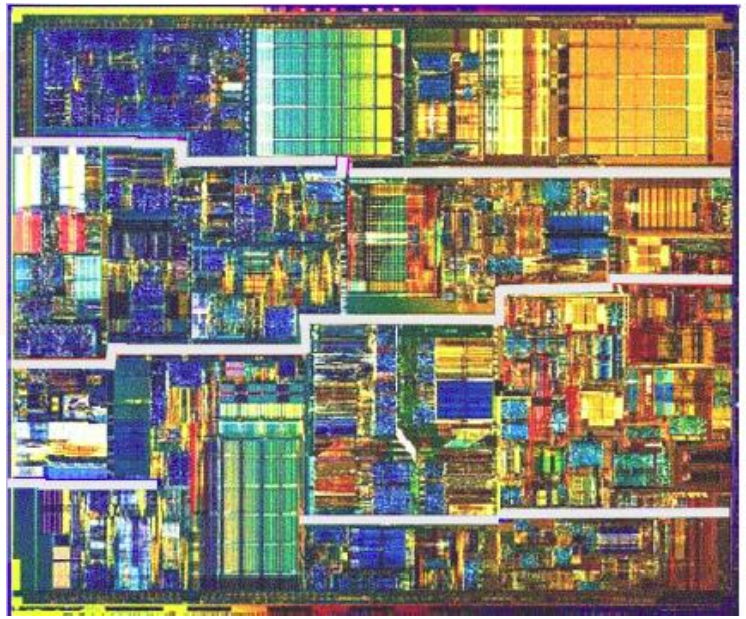


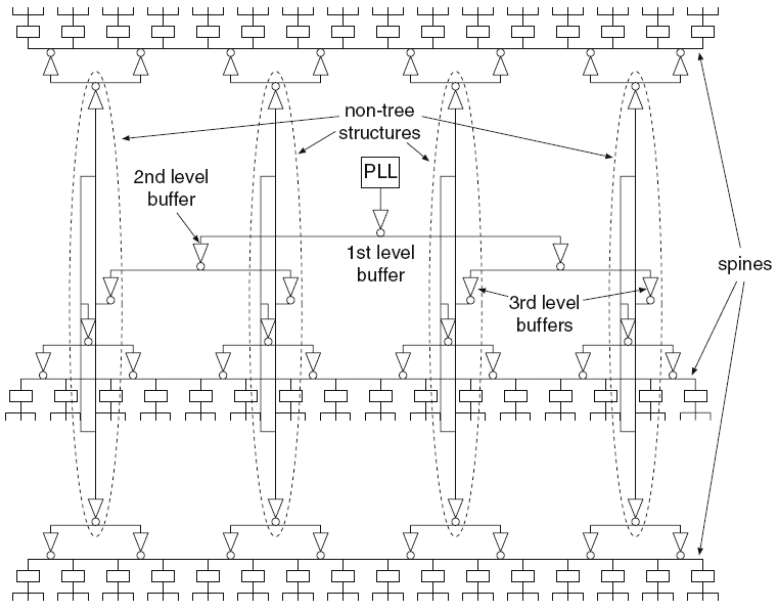




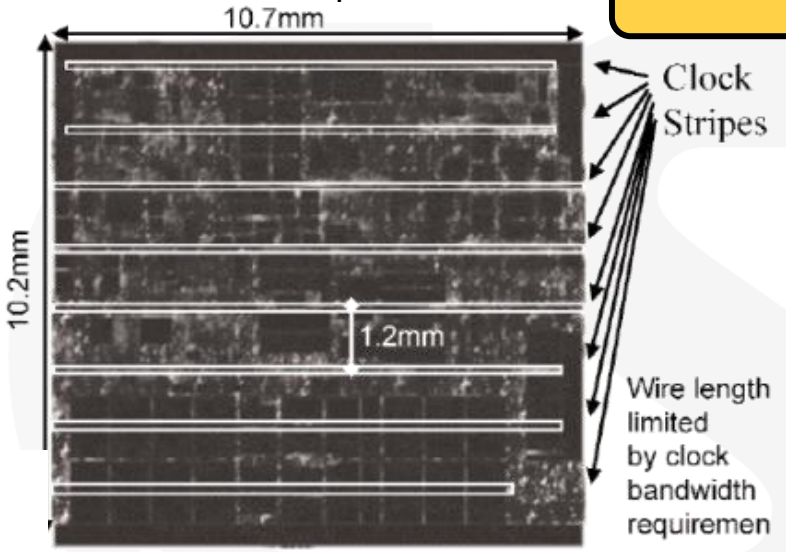
Clock Spines

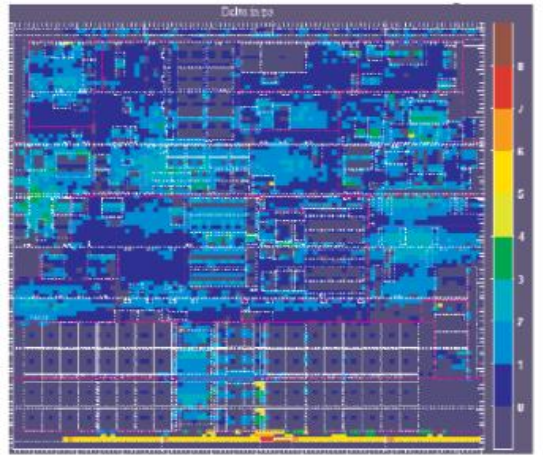
- **Clock grids are too power (and routing) hungry.**
- **A different approach is to use spines**
  - Build an H-Tree to each spine
  - Radiate local clock distribution from spines
- **Pentium 4 (2001) used the clock spine approach.**





Later Pentium 4's used more spines





delay in ps

Source: Bindal ISSCC 2003

Summary of main clock dist. approaches

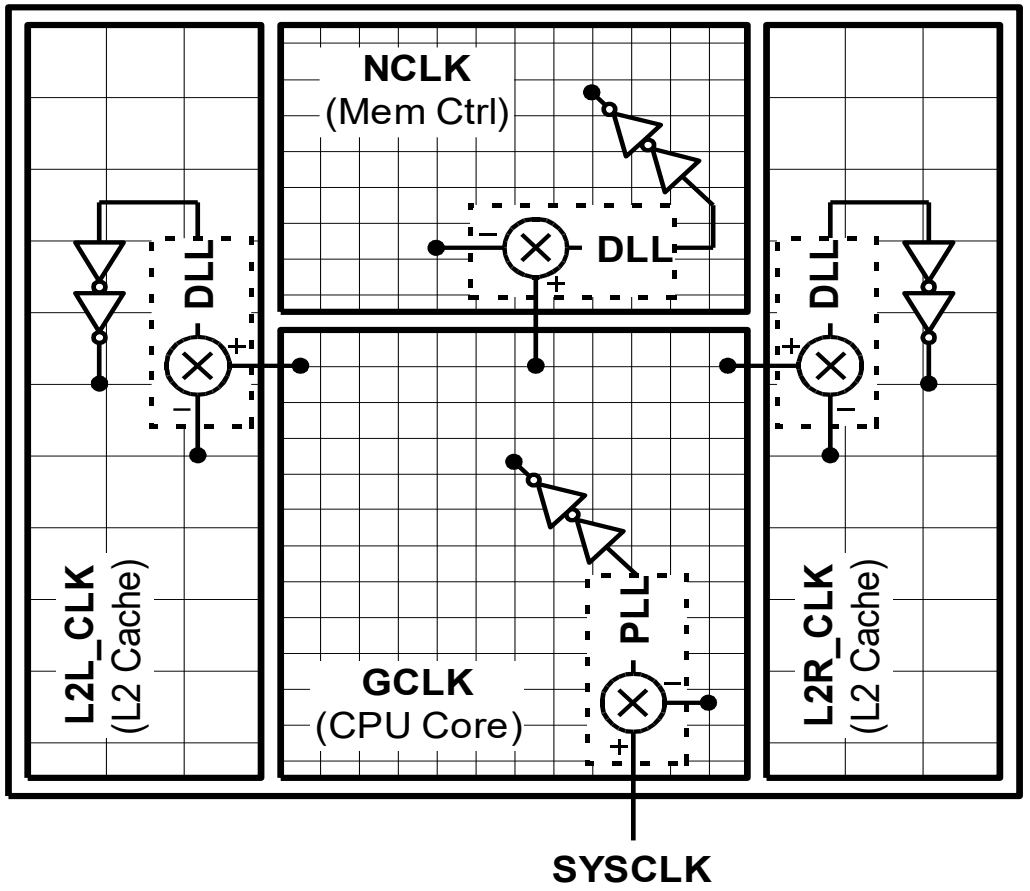
Three basic routing structures for global clock:

- **H-tree**
  - Low skew, smallest routing capacitance, low power
  - Floorplan flexibility is poor.
- **Grid or mesh**
  - Low skew, increases routing capacitance, worse power
  - Alpha uses global clock grid and regional clock grids
- **Spine**
  - Small RC delay because of large spine width
  - Spine has to balance delays; difficult problem
  - Routing cap lower than grid but may be higher than H-tree.

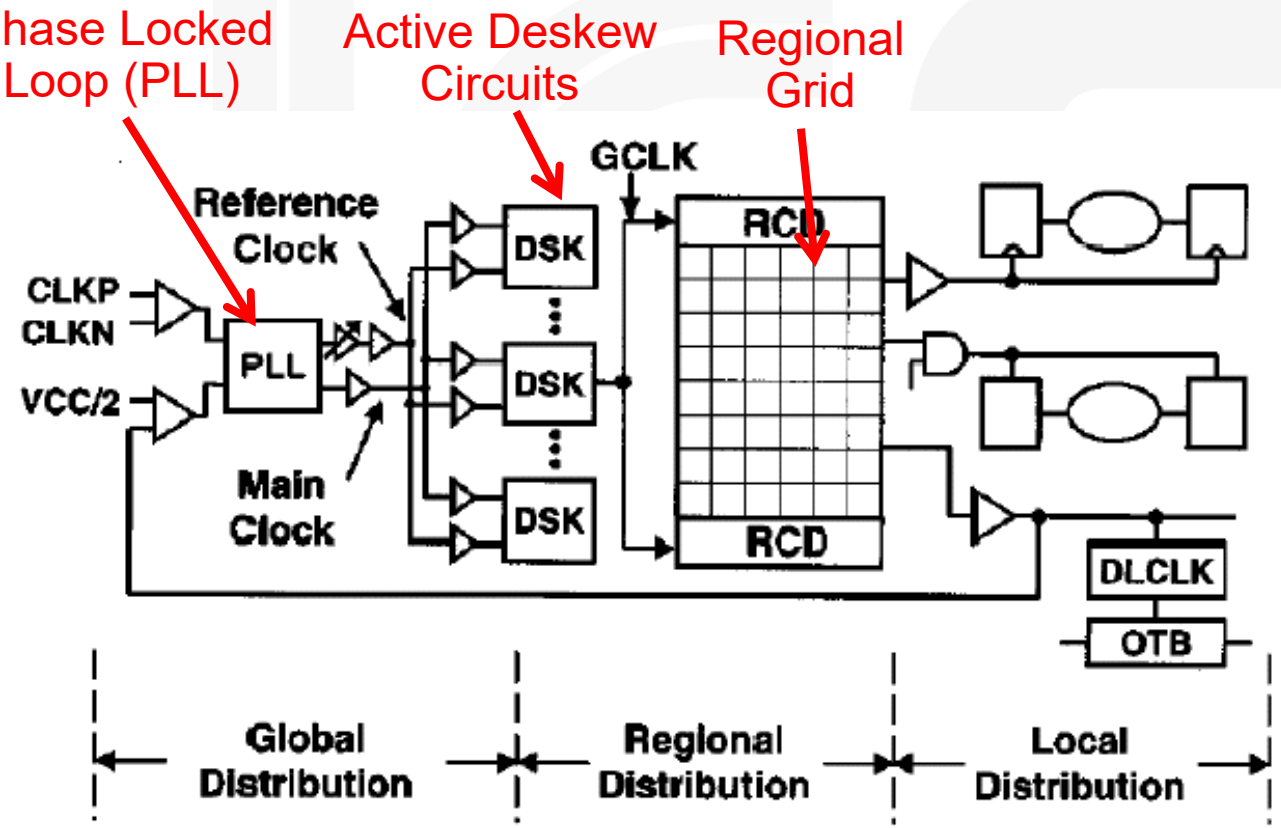
Structure	Skew	Cap/area/ power	Floorplan Flexibility
H-Tree	Low/Med	Low	Low
Grid	Low	High	High
Spine	High	Medium	Medium

Active Skew Management (Deskewing)

- Alpha EV7

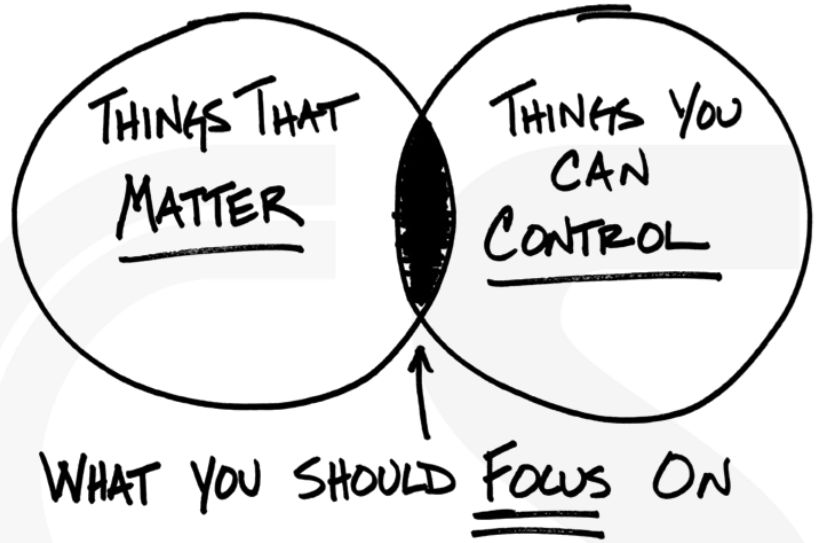


- Intel Itanium



Clock Concurrent Optimization

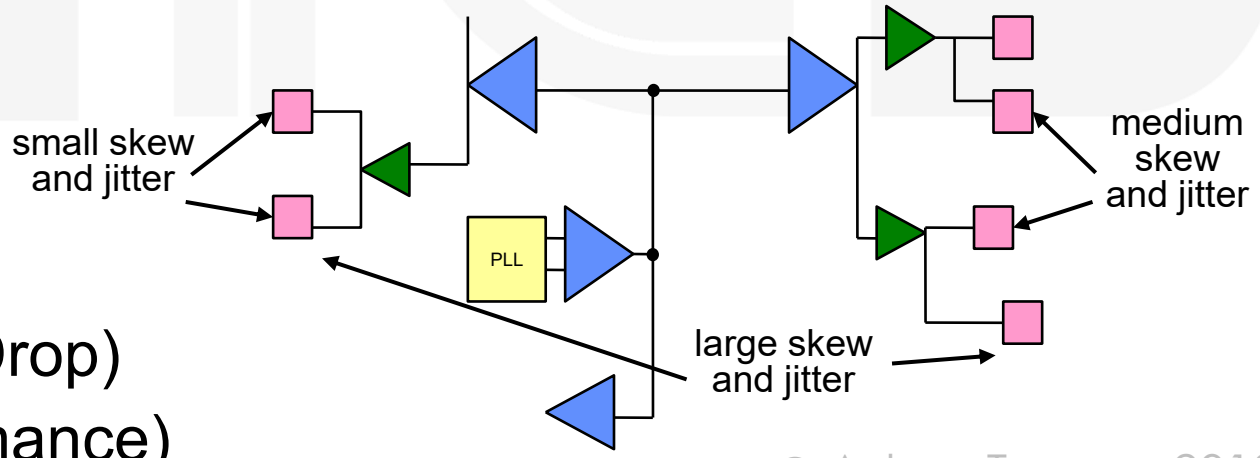
- **What is the main goal of CTS?**
  - We are trying as hard as we can to minimize skew.
  - And on the way, we are burning power, wasting area, suffering from high insertion delay, etc.
  - ***But is minimal skew our actual goal***?
  - Why are we minimizing skew in the first place?



- **Maybe we should forget about skew and focus on our real goals?**
  - We need to **meet timing** and DRV constraints.
  - Minimizing skew was just to correlate post-CTS and pre-CTS timing.
  - But maybe we should just *consider timing*, while building our clock tree.
- **This new approach is known as Clock Concurrent Optimization (CCOpt)**

Clock Concurrent Optimization

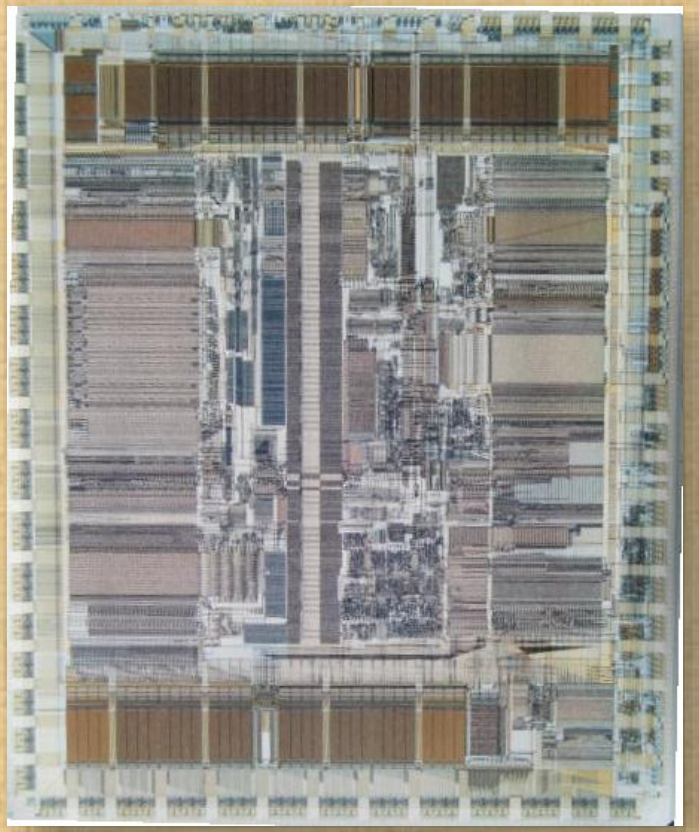
- **CCOpt Methodology:**
  - First, build a clock tree, in order to fix DRVs.
  - Then check timing (setup and hold) and fix any violations.
- **Why is this a good approach?**
  - Most timing paths are local.
  - Therefore, they probably come from the same clock branch and don't need much skew balancing to start with.
- **Less skew balancing leads to:**
  - Lower insertion delay (power, jitter)
  - Fewer clock buffers (power, area)
  - Distribution of peak current (less IR Drop)
  - A heavy dose of useful skew (performance)



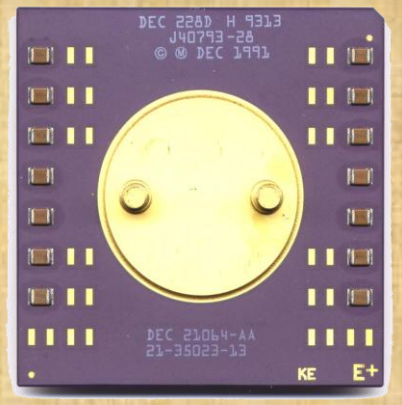
The Chip Hall of Fame

- **Digital introduced a ton of novelty, including clocking, with the Alpha architecture, starting with the**

DEC Alpha 21064



- 21064 = "A 21st Century ready, 64-bit, gen. 0 uarchitecture.
- Release date: 1992 64 bit Alpha Architecture
- Process: Digital Equipment Co. CMOS-4 0.75um
- 3-metal layers, 3.3V power supply, 150-200 MHz
- 1.6 Million Transistors , 232 mm^2 die size, price $3,375
- At the time of introduction, the Alphas were the world's fastest chips.
- Phased out after DEC was acquired by Compaq in 1998 and chose to use Intel Itanium architecture, instead.

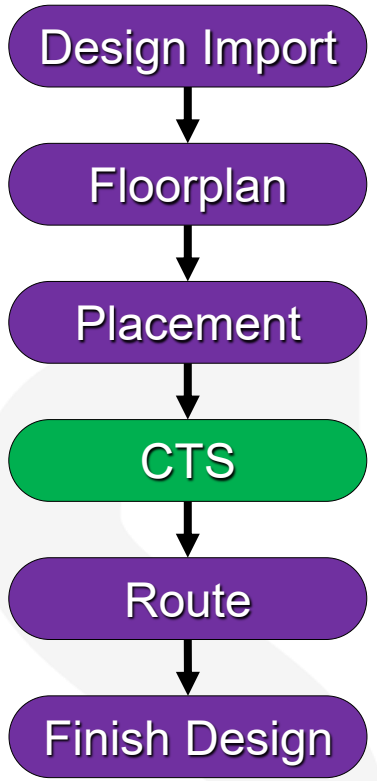


Not yet inducted to the IEEE Chip Hall of Fame

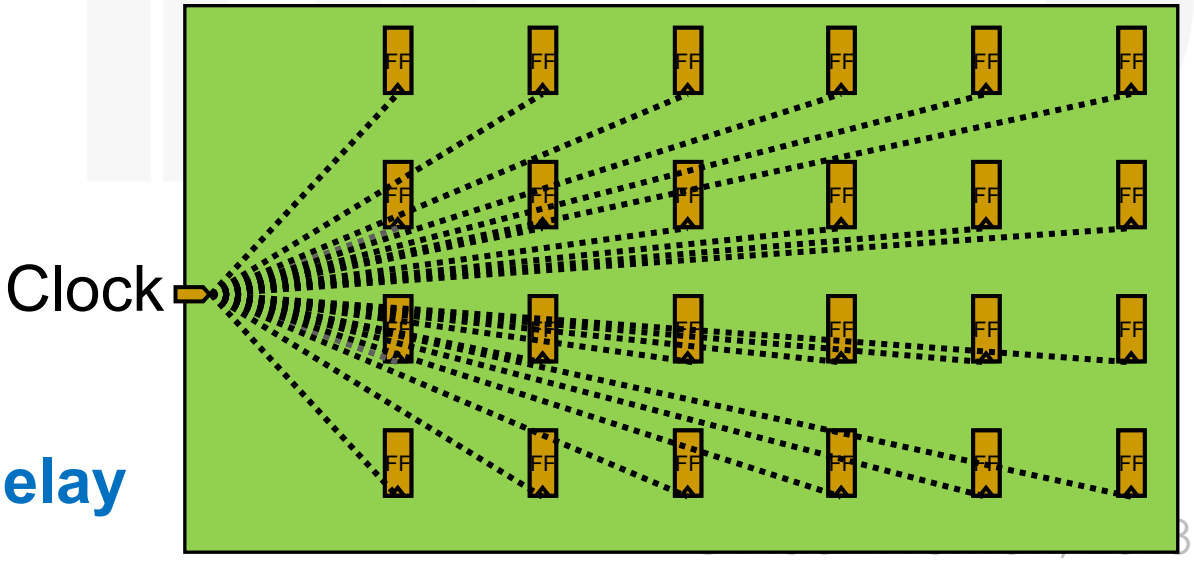
Clock Tree Synthesis in EDA

Starting Point Before CTS

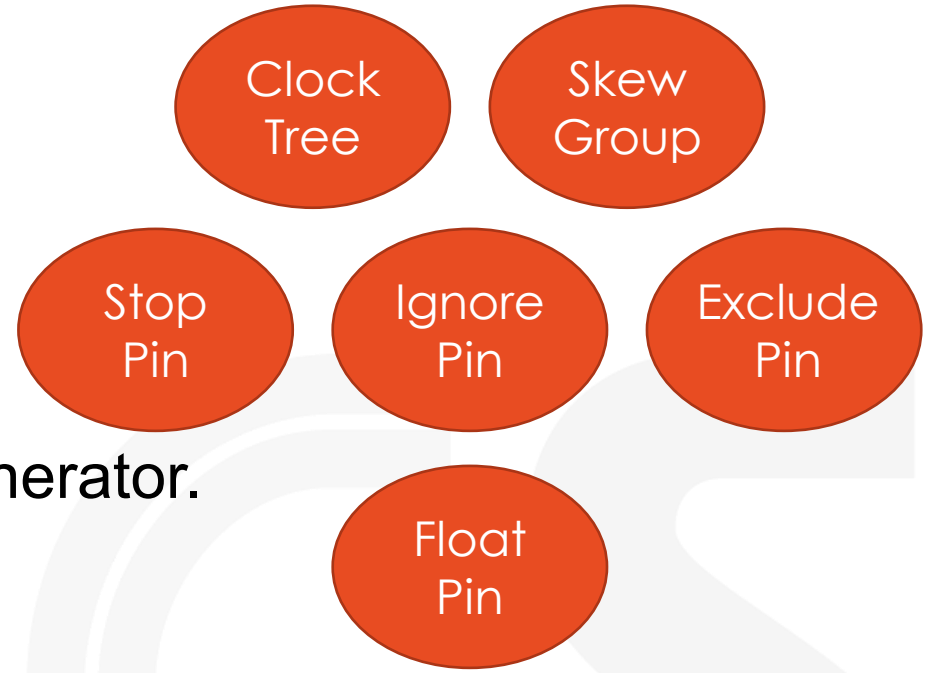
DRV = Design Rule Violations



- **So remember:**
  - Our design is placed, and therefore, we know the location of all clock sinks (register and macro clock pins)
  - All clock pins are driven by a single clock source, which we considered ideal until now.
  - We may have several clocks and some logic on the clock network, such as clock gates, muxes, clock dividers, etc.
- **We must now buffer the clock nets to:**
  - Meet **DRV** constraints:
    - Max **fanout**, max **capacitance**, max **transition**, max **length**
  - Meet clocking goals:
    - Minimum **skew**, minimum **insertion delay**



Some basic understanding



- **What makes up a clock tree?**
  - A starting point
    - The clock port or the output pin of the clock generator.
  - Leaf/end points
    - Clock pins of registers, memories, etc.
  - Buffers/Inverters
    - Required to ensure clock transitions and meet skew requirements.
  - Special logic
    - Such as multiplexers, integrated clock gates, clock dividers
- **We need a "language" to define these (and other) components**
  - The following slides will introduce you to the CCOpt naming conventions for these elements.

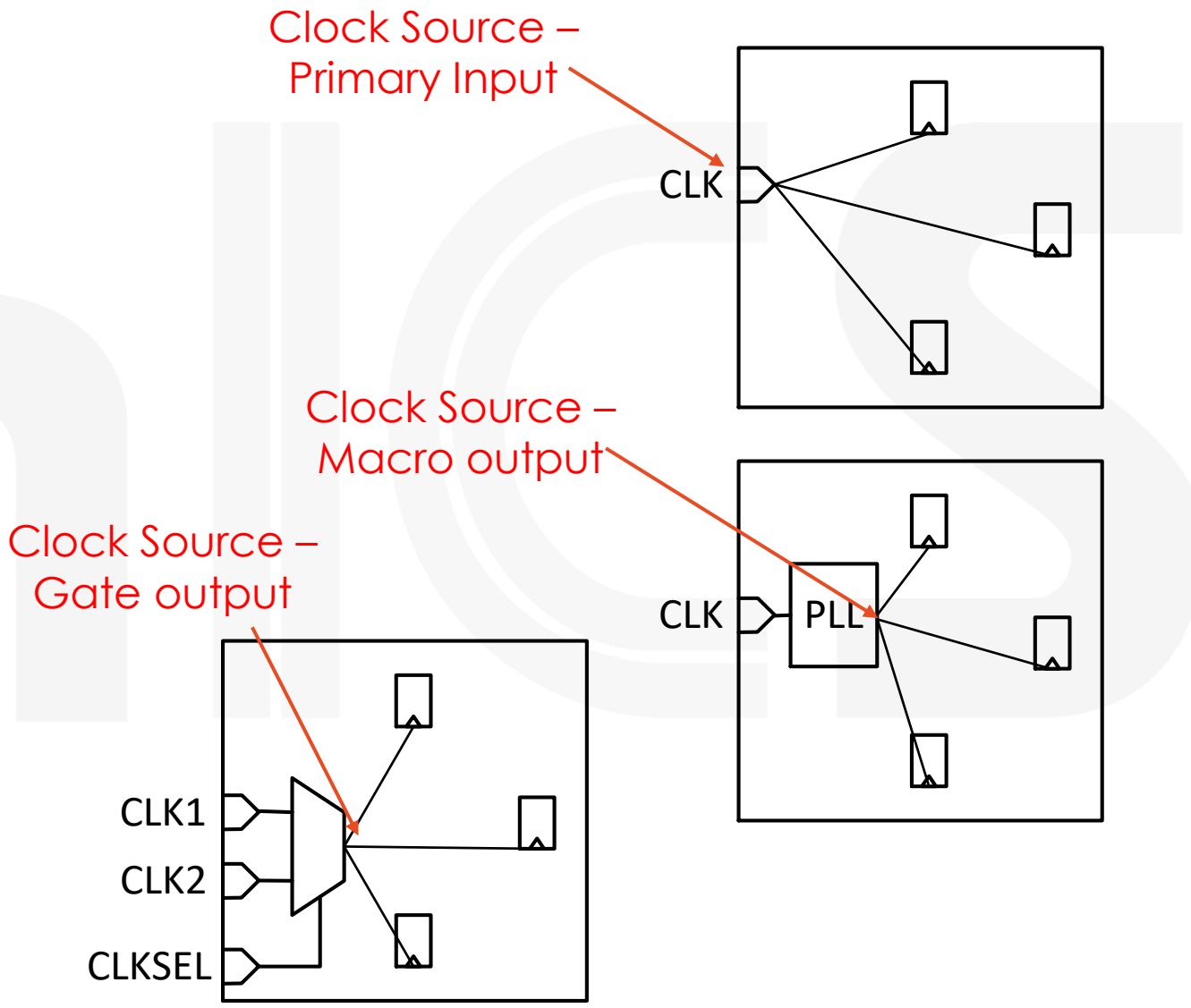
CTS Definitions – Sources and Sinks

Clock Source

- The pin that a clock fans out from.
- This can be:
  - A primary input (port) to our design
  - An output pin of an IP (e.g., PLL)
  - An output pin of a gate (e.g., clock mux, clock gate).

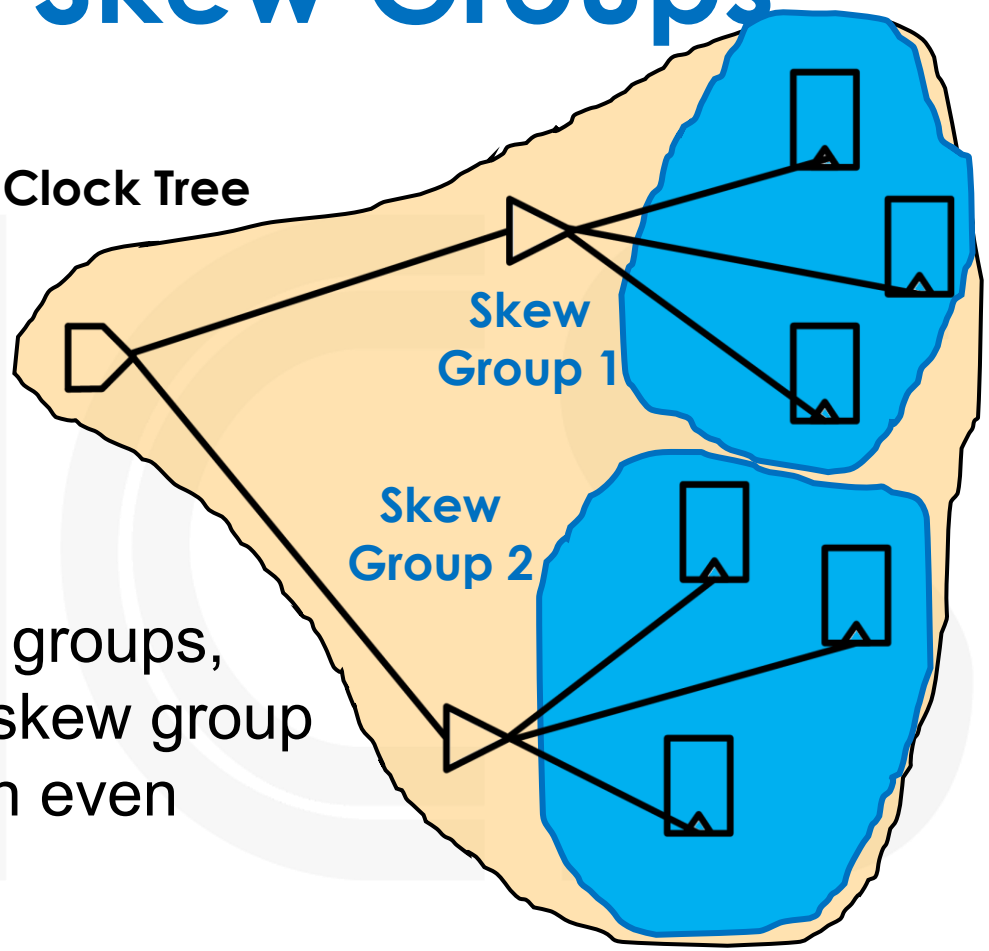
Clock Sink

- All pins that receive the clock signal.
- This can be:
  - Clock input of a register (FF, latch)
  - Clock input of an IP (e.g., SRAM)
  - Primary output (if the clock is driven outside the block)



CTS Definitions – Trees and Skew Groups

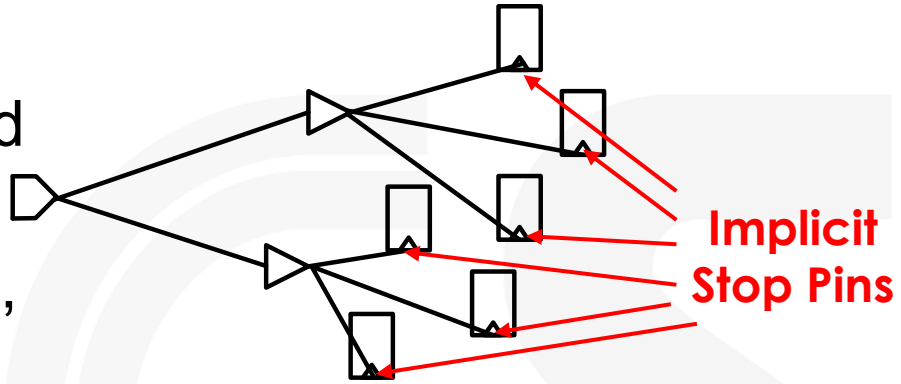
- **Clock Tree**
  - The root of a circuit graph for buffering.
- **Skew Group**
  - A subset of clock sinks to consider for skew balancing/analysis. By default, all the sinks of a clock tree are in the same skew group.
  - However, they can be divided into several skew groups, sinks of several clocks can belong to the same skew group (e.g., clock and generated clock), and a sink can even belong to more than one skew group.
- **Basic CCOpt Commands:**




```
create_clock_tree -name clk -source [get_ports CLK] -no_skew_group
create_skew_group -name clk -sources [get_ports CLK] -auto_sinks
update_skew_group -skew_group clk -add_sinks [get_pins FF1/CK]
```

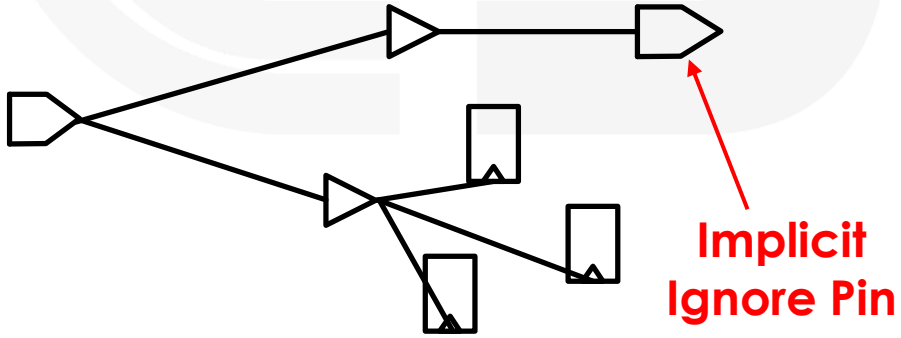
CTS Definitions – Stop/Ignore/Exclude Pins

- **Stop Pins**
  - A leaf of a clock tree. The clock net will be buffered up to the stop pin but not beyond it.
  - All clock sinks are implicit stop pins, and therefore, will be considered for skew balancing/analysis.
  - To define additional pins as stop pins in CCOpt, use:




```
set_db pin:INV1/A .cts_sink_type stop
```

- **Ignore Pins**
  - Ignore pins are pins on the clock net that will not be considered a sink in any skew group.
  - The clock net will be buffered up to the ignore pin but not beyond it.



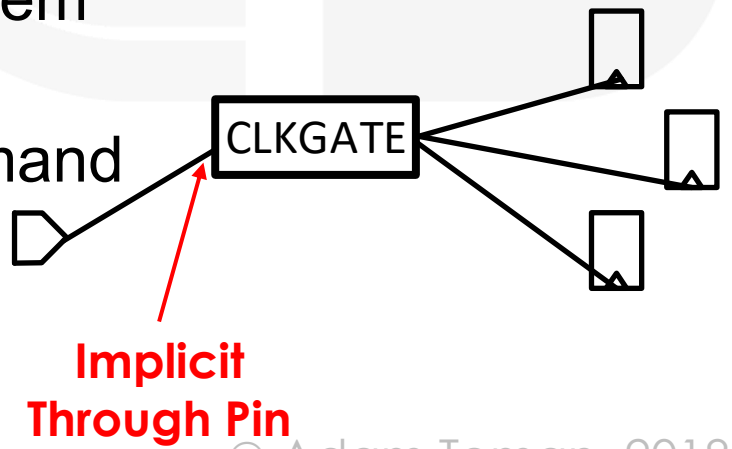

```
set_db pin:div_ff1/CK .cts_sink_type ignore
```

CTS Definitions – Stop/Ignore/Exclude Pins

- **Exclude Pins**
  - Exclude pins are similar to ignore pins, but the clock net will not be buffered up to an exclude pin.

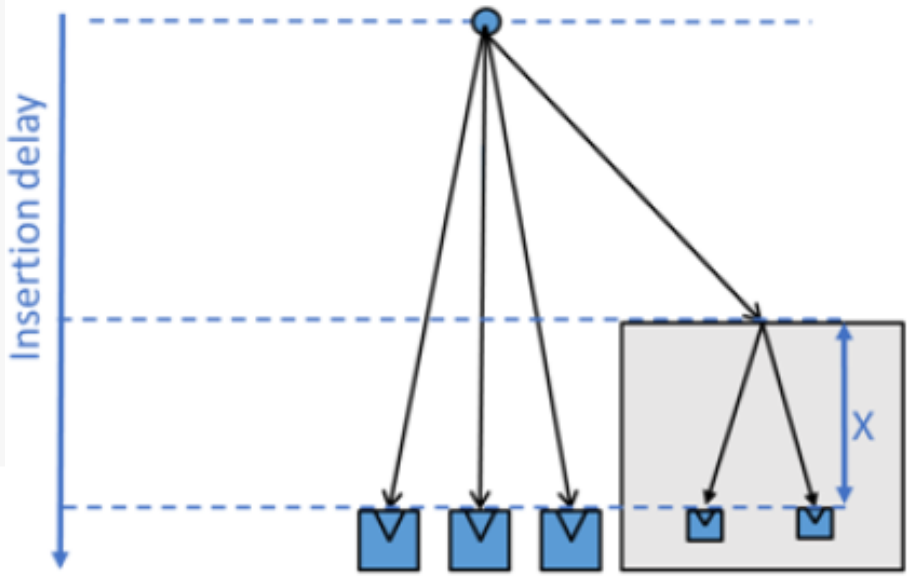
```
set_db pin:div_ff1/CK .cts_sink_type exclude
```

- **Through Pins**
  - Through pins are pins, which would otherwise be considered stop pins, but we want the clock to propagate through them (for buffering and adding pins to the skew group).
  - In the new versions of Innovus, there is no explicit command to define a through pin. Just call it an ignore pin…



CTS Definitions – Insertion Delay Pin

- **In some cases, we would like to provide the clock to a certain stop pin *earlier* or *later* than the *average insertion delay*.**
  - For example, if a macro block has some internal insertion delay, we would like to provide the clock early for skew balancing.
- **Such a pin is also known as a "float pin"**



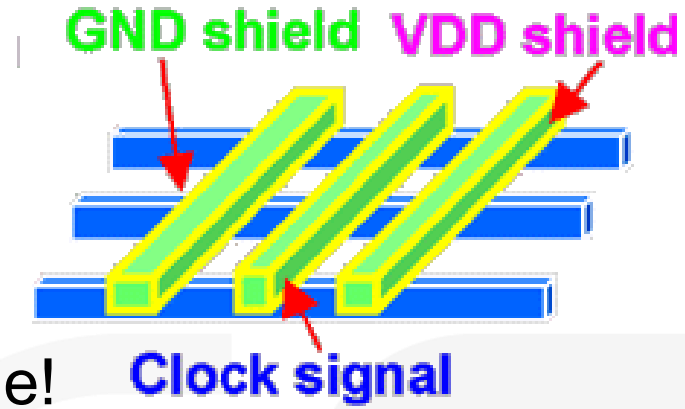
- **For example, to provide the clock to an SRAM called "mem"150ps *earlier* than the average insertion delay :**

```
set_db pin:mem/CK .cts_pin_insertion_delay 150ps
```

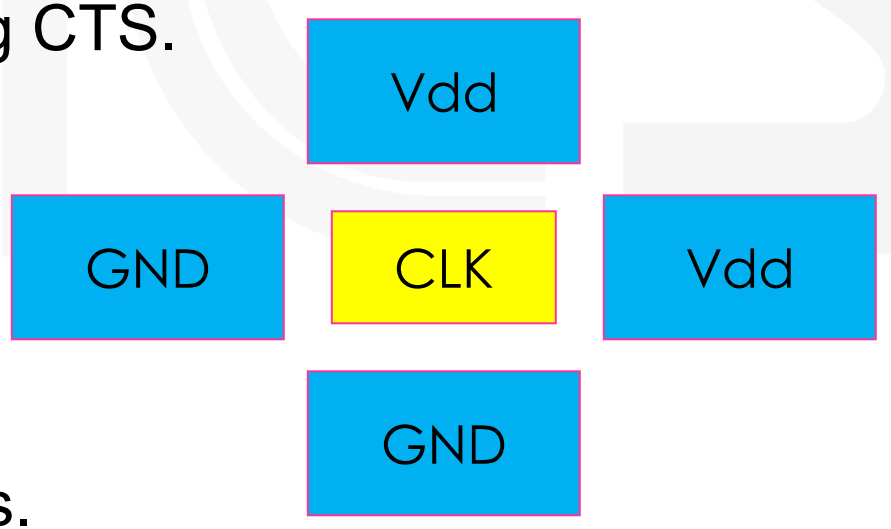
CTS Definitions – Pin Type Summary

	Part of the Clock Tree	Considered for DRV fixing	Considered for Delay Balancing	Clock propagates beyond it
Stop Pin	Yes	Yes	Yes	No
Ignore Pin	Yes	Yes	No	No
Exclude Pin	No	No	No	No
Float Pin (insertion_delay)	Yes	Yes	Yes – according to constraint	No

Clock Net Routing



- **Clock nets are *very* important in terms of signal integrity**
  - A **glitch** on a clock net will cause an additional clock edge!
  - Slow transitions will cause deteriorated setup/hold times of registers.
  - Fast transitions are strong aggressors to neighboring nets.
- **Therefore:**
  - We will usually *pre-route* the clock nets during CTS.
    - First choice of routing tracks
  - Use higher, thicker metals for clock routing
    - Lower resistance
    - Less capacitance to the substrate
  - Apply **shielding** to clock nets!
  - Consider adding DeCaps next to clock buffers.



How do we route clock nets?

- **In Innovus, we can define special routing rules for specific nets:**
  - These are called Non-Default Rules (NDRs)
  - For example, double-width or double-spacing.
- **We can tell Innovus to use a certain NDR, by creating a Routing Type**
  - The routing type enables us to define preferred layers and shielding.
- **In Innovus, we differentiate between three types of clock nets:**
  - **Top** – The initial branch of the clock tree. Very wide and high.
  - **Trunks** – The main branches of the clock tree. Wide and high.
  - **Leaf** – The bottom levels of the clock tree. Closer to the logic.
- **So, we will define NDRs and routing rules and then apply them to clock nets.**

Shielding and Non-Default Routing Rules

- **First, define non-default routing rules (NDR):**
  - Double width and double spacing

```
create_route_rule –name CTS_2W2S \
      –spacing_multiplier 2   –width_multiplier 2
```

- **Then, create a routing type for CTS**

```
create_route_type –name cts_trunk –non_default_rule CTS_2W2S \
      -top_preferred_layer M7 –bottom_preferred_layer M6 \
      -shield_net VSS –bottom_shield_layer M6
```

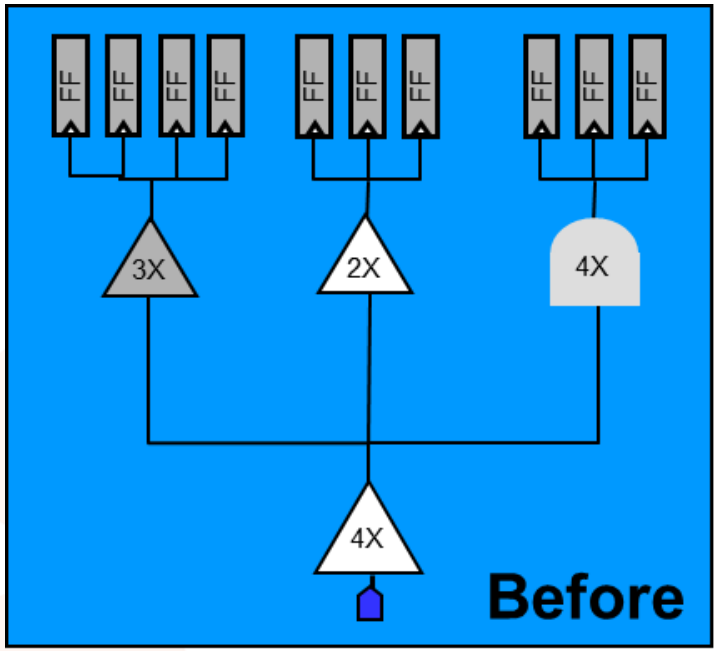
- **Finally, apply property to *trunk* type clock nets**

```
set_db cts_route_type_trunk cts_trunk
```

Analyzing Clock Trees

- **Before running clock tree synthesis, analyze each clock tree in the design to determine:**
  - What the clock root is.
  - What the desired clock sinks and clock tree exceptions are.
  - Whether the clock tree contains preexisting cells, such as clock gating cells.
  - Whether the clock tree converges, either with itself (a convergent clock path) or with another clock tree (an overlapping clock path).
  - Whether the clock tree has timing relationships with other clock trees in the design, such as inter-clock skew requirements.
  - What the DRV constraints are (maximum fanout, maximum transition time, and maximum capacitance).
  - What are the library cells to use for implementing the clock tree.
  - What the routing constraints (routing rules and metal layers) are.

Clock Tree Optimizations



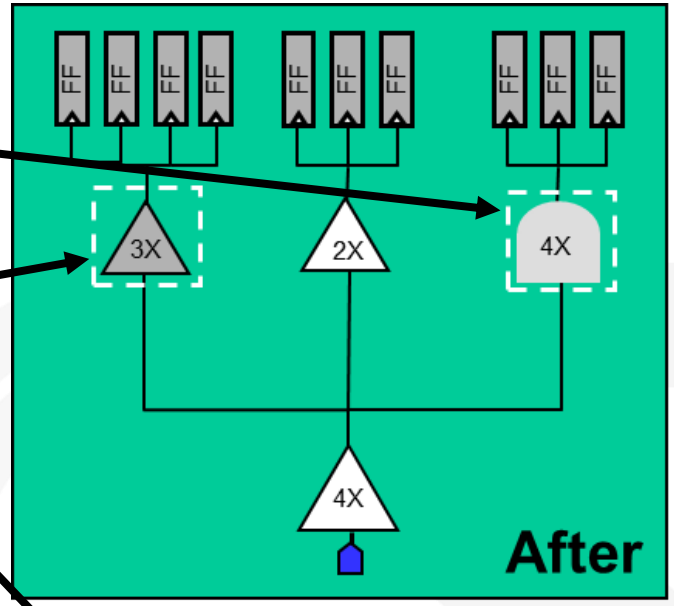
Gate relocation

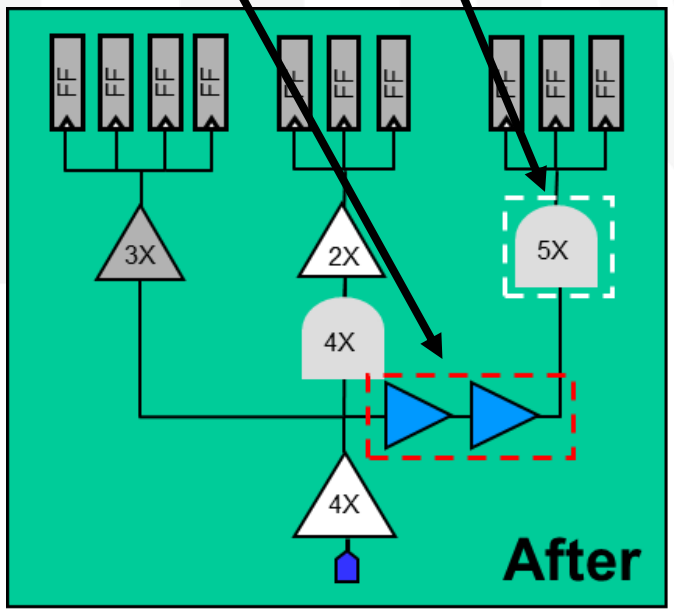
Buffer relocation

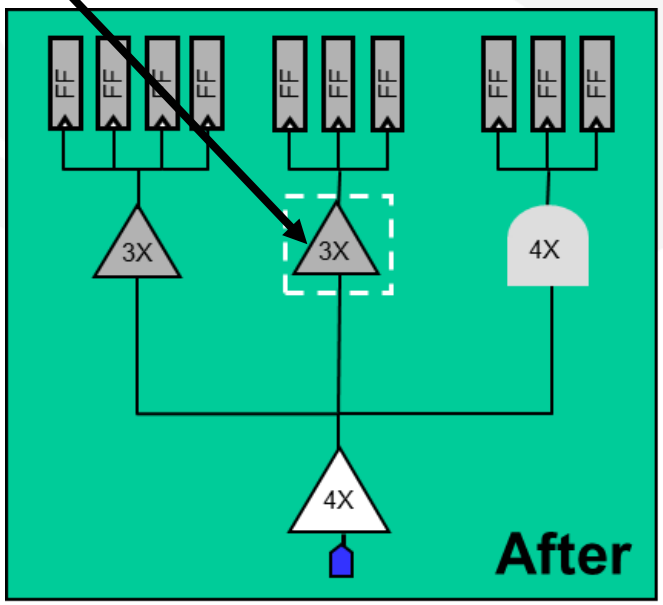
Buffer sizing

Delay insertion

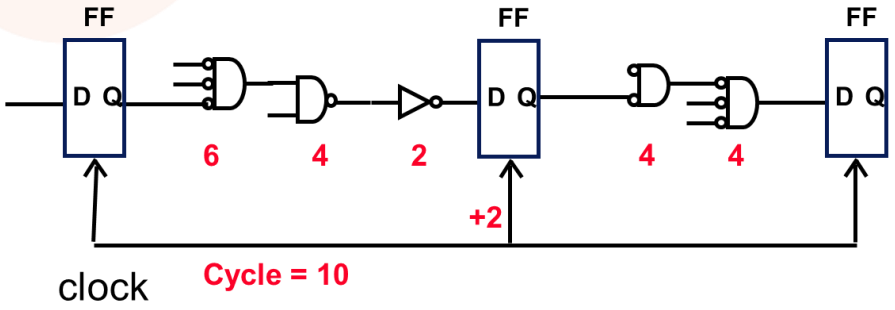
Gate sizing







Useful Skew

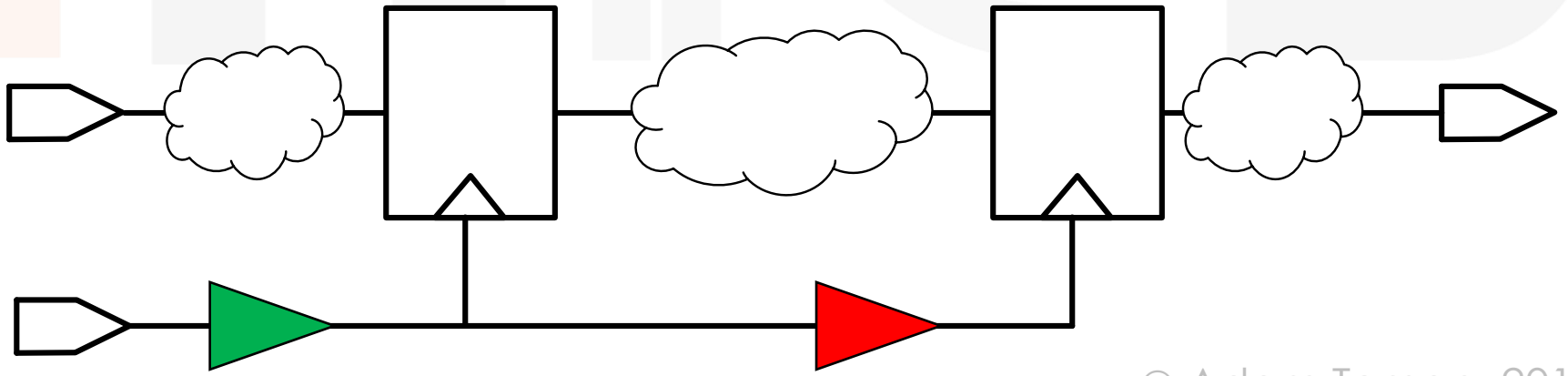


Issue with Post CTS Interface Timing

- **Before CTS, clock is ideal.**
  - We define I/O constraints without thinking about the clock influence

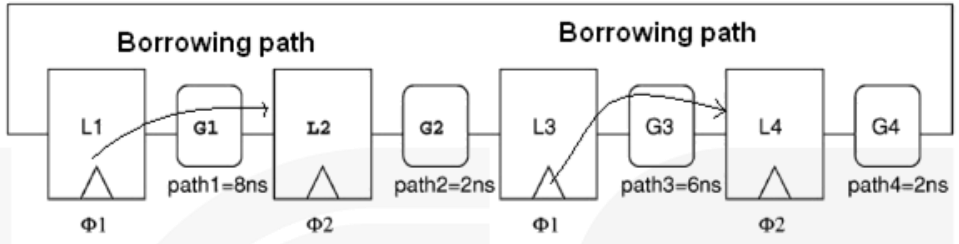
```
set_input_delay -clock clk $IN_DLY [all_inputs]
set_output_delay -clock clk $OUT_DLY [all_outputs]
```

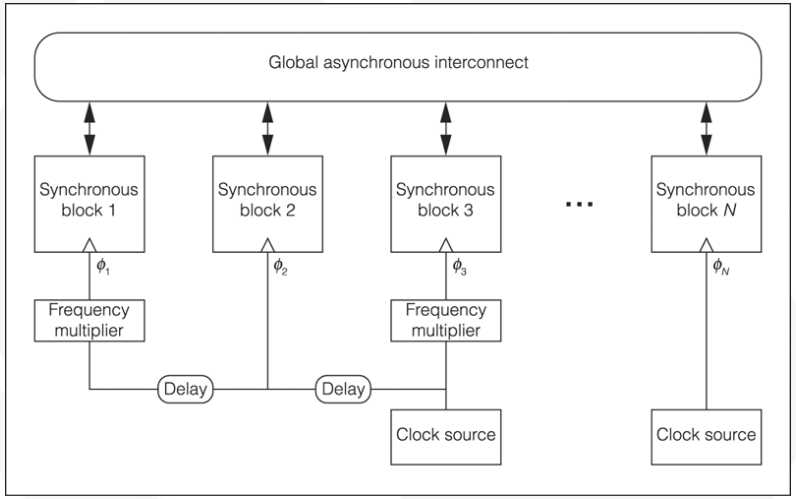
- **But after CTS:**
  - We added positive skew to the `in2reg` paths.
  - We added negative skew to the `reg2out` paths.
- **Therefore:**
  - Add the average insertion delay to the clock paths to the I/O ports.



Reducing Clock Distribution Problems

- **Use latch-based design**
  - Time borrowing helps reduce impact of clock uncertainty
  - Timing analysis is more difficult
  - Rarely used in fully synthesized ASICs, but sometimes in datapaths of otherwise synthesized ASICs



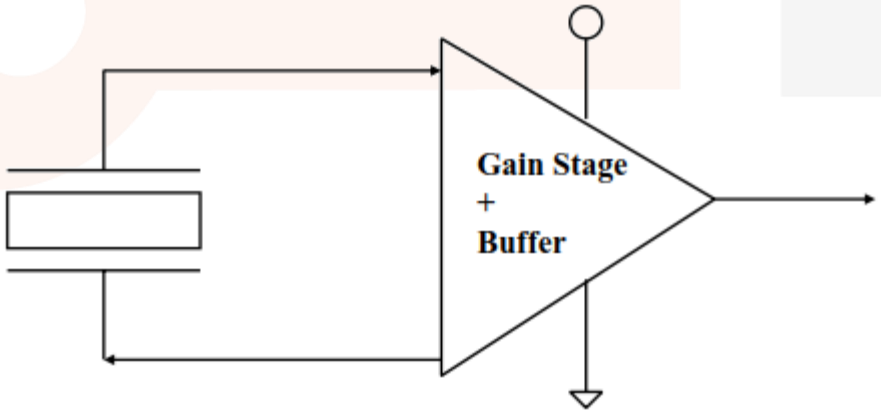


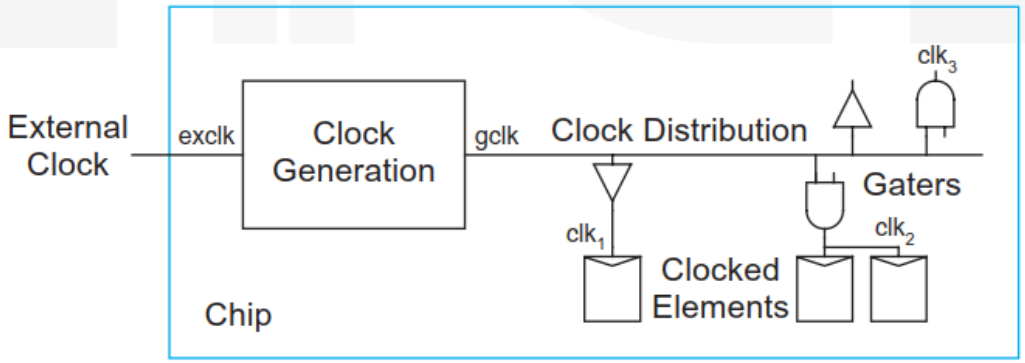
- **Make logical partitioning match physical partitioning**
  - Limits global communication where skew is usually the worst
  - Helps break distribution problem into smaller sub-problems
- **Use globally asynchronous, locally synchronous design**
  - Divides design into synchronous regions which communicate through asynchronous channels
  - Requires overhead for inter-domain communication
- **Use asynchronous design**
  - Avoids clocks all together
  - Incurs its own forms of control overhead

Additional Subjects: Clock Generation

Clock Generation

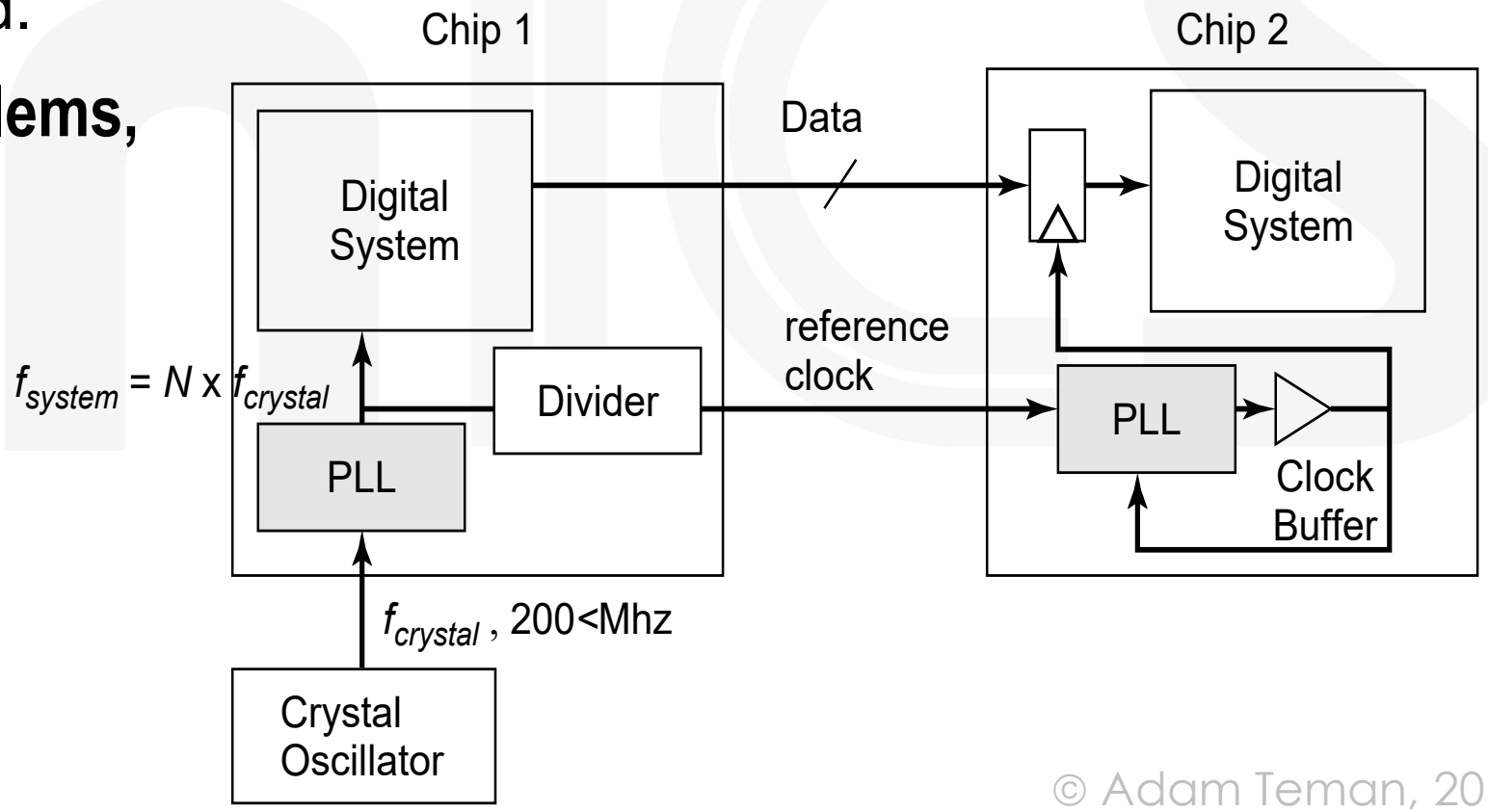
- **Where does the clock come from?**
  - The easiest way to generate a clock is by using a ring oscillator or some other non-stable circuit, but these are susceptible to PVT variations.
  - Therefore, clocks are generally generated off-chip using a crystal and an oscillation circuit.
  - However, usually only one off-chip clock can be used (a single frequency) and the frequency that can be input to the chip is limited to around 100 MHz.
  - Therefore, on-chip local clock generation is employed, usually with a PLL or DLL.





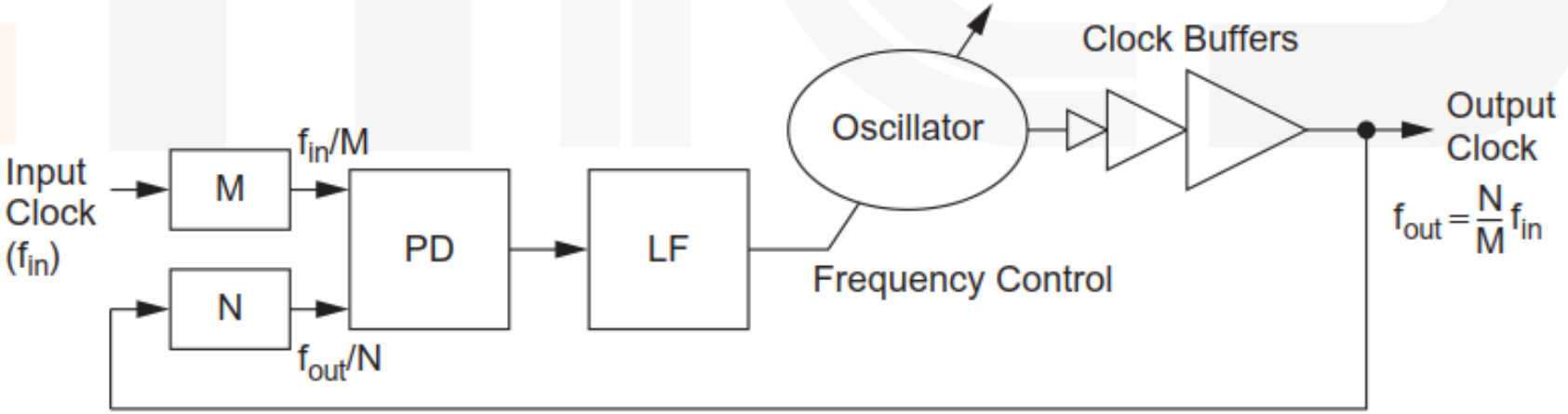
Local Clock Generation

- **Externally generated clocks suffer from two primary problems:**
  - Frequency is limited, i.e., a *clock multiplier* is needed.
  - Clock phase is uncontrolled, such that communication with the external clock domain is unsynchronized.
- **To solve both of these problems, a Phase-Locked Loop (PLL) is used.**
  - If clock multiplication is not required, a delay-locked loop (DLL) is a more simple solution.



Local Clock Generation

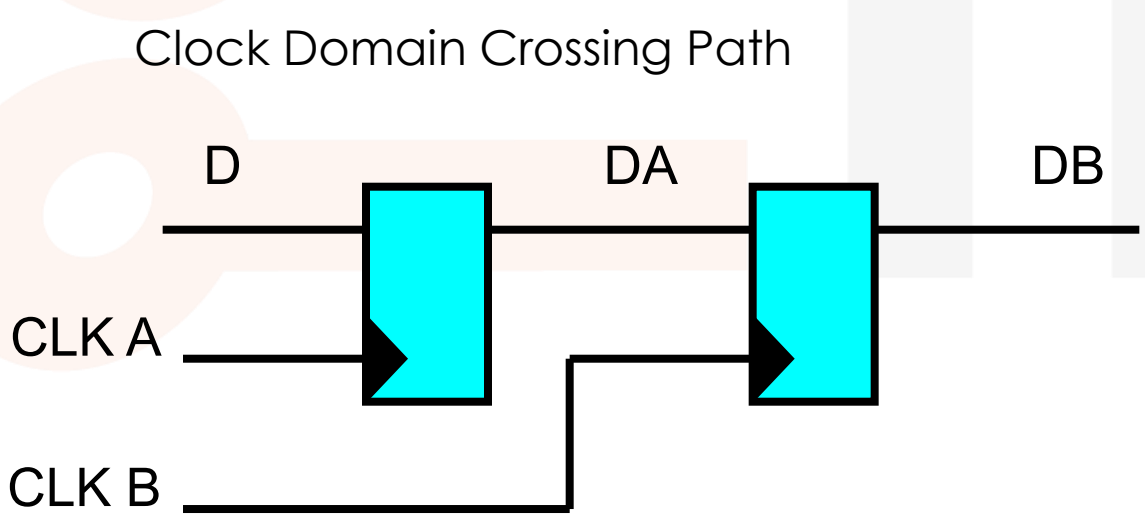
- **How does a PLL work?**
  - A *phase detector* (**PD**) produces a signal proportional to the phase difference between the input and output clocks.
  - A *loop filter* (**LF**) converts the phase error into a control signal (voltage).
  - A *voltage-controlled oscillator* (**VCO**), creates a new clock signal based on the error signal.
- **What about a DLL?**
  - Same principle, but instead of changing the frequency, it just delays the clock until the phase is equal.

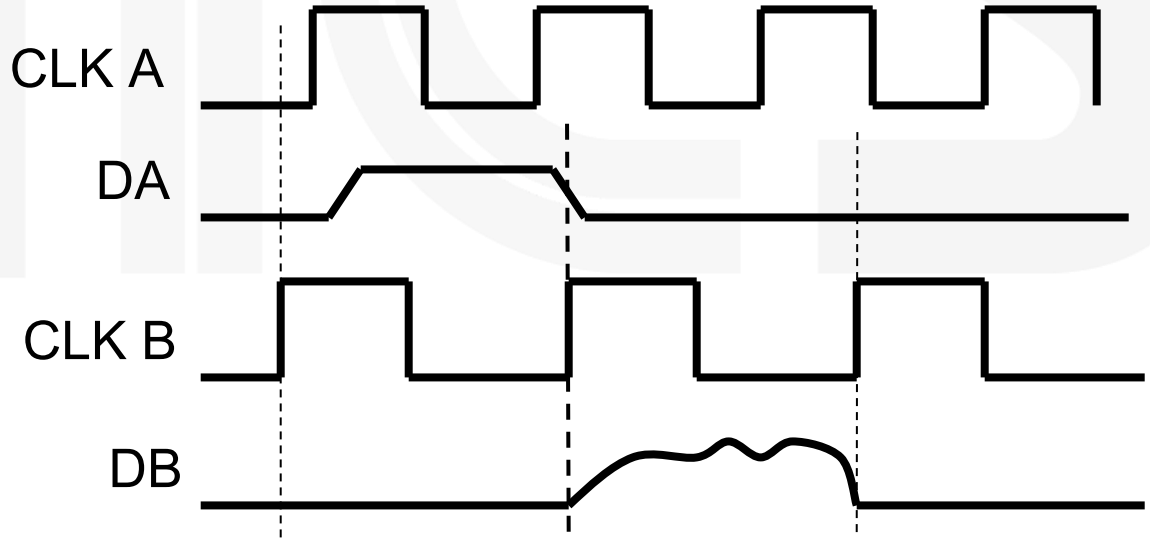


Additional Subjects:
Clock Domain Crossing

Clock Domain Crossing (CDC)

- **Most system-on-chips have several components that communicate with different external interfaces and run on different clock frequencies.**
  - In other words, they have multiple *asynchronous clock domains*.
- **Asynchronous clocks cannot communicate with each other in a straightforward fashion:**





Problems with CDC

The main problems with passing data between asynchronous domains are:

- **Metastability:**
  - A setup/hold violation in the capture register. May cause:
    - High propagation delay at the fanout.
    - High current flow in the chip (even burnout).
    - Different values of the signal at different parts of the fanout.
- **Data Loss:**
  - New data in the source may be generated w/o the data being captured by the destination.
- **Data Incoherency:**
  - Data may be captured late, causing several coherent signals to be in different states.

What is the probability of metastability?

Let us define:

T_w – an error window (setup+hold) around the clock cycle

f – clock frequency

f_D – Frequency of data change

Now assume that a data (D) change can come anywhere in the clock cycle relative to the capture clock, so:

$$Rate(\text{meta}) = f \cdot f_D \cdot T_w$$

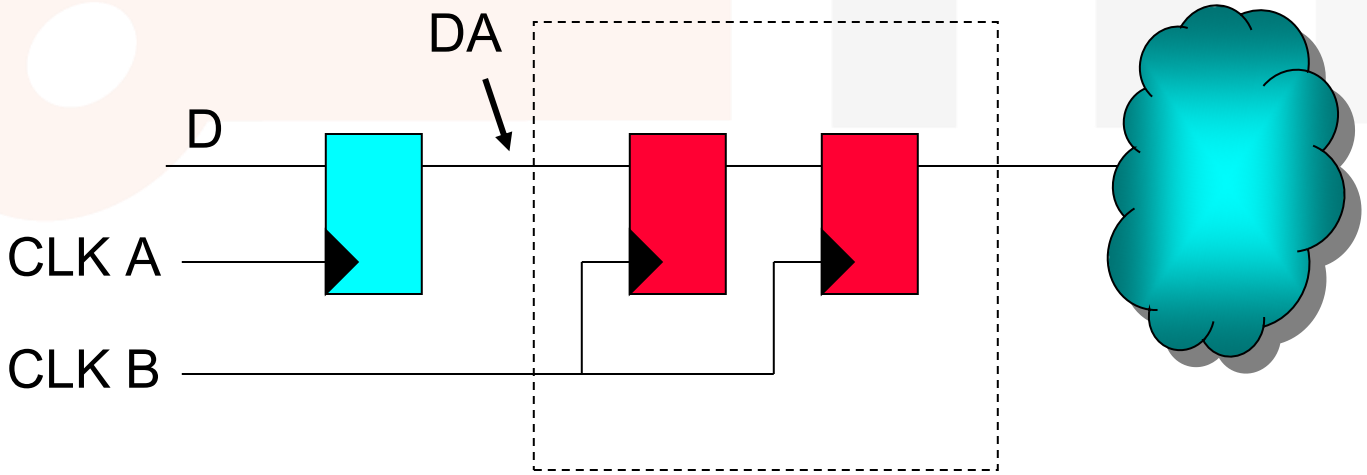
Assume:

$$f = 1\text{GHz} \quad f_D = 0.1f \quad T_w = 20\text{ps}$$

$$Rate(\text{meta}) = 2 \cdot 10^6 / \text{sec}$$

Solutions: Synchronizers

- **By cascading two or more flip flops, we create a simple *synchronizer*.**
  - The signal has one (or more) clock cycles to stabilize.
  - However, there is a probability that the signal will not settle within the cycle time (T).



What is the probability of failure?

The probability for metastability to pass is:

$$P(t > S) = e^{-S/\tau}$$

with τ a parameter of the flip flop

We want the metastability to dissipate at least t_{setup} before the next clock edge, so:

$$P(\text{failure}) = P(\text{meta}) \cdot P(\text{exit}) = \frac{T_w}{T} \cdot e^{-\frac{T - t_{setup}}{\tau}}$$

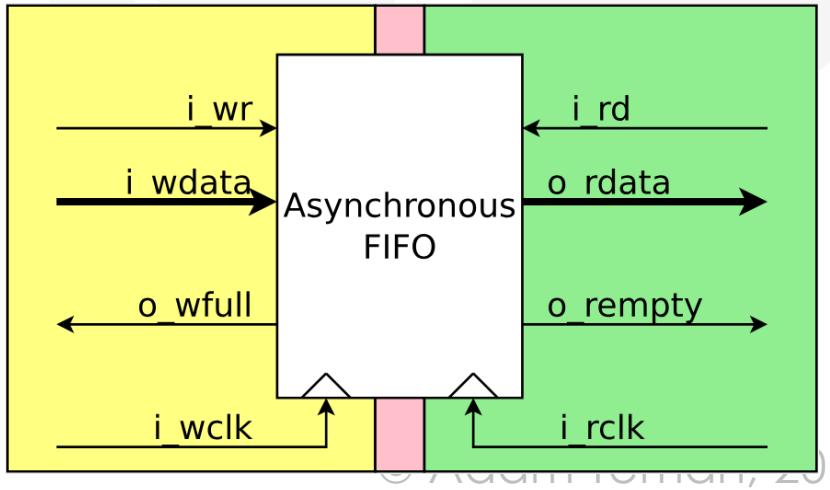
And the mean time between failures (MTBF) is the inverse of the failure rate:

$$MTBF = \frac{1}{Rate(\text{failure})} = \frac{1}{f \cdot f_D \cdot T_w} e^{-\frac{T - t_{setup}}{\tau}}$$

For our previous example, this is about 10^{24} years…

Are synchronizers enough?

- **No!**
  - We may have taken care of metastability, but data loss and data incoherence are still there.
  - So we need to design our logic accordingly.
- **To eliminate data loss:**
  - Slow to fast clock – we won't lose any data.
  - Fast to slow clock – hold source data for several cycles.
- **But for data coherence, we need more thinking:**
  - Handshake protocols.
  - First-in First-out (FIFO) interfaces
  - Other solutions (Gray code, Multiplexers, etc.)



Source: ZipCPU.com

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