

Practice 3:

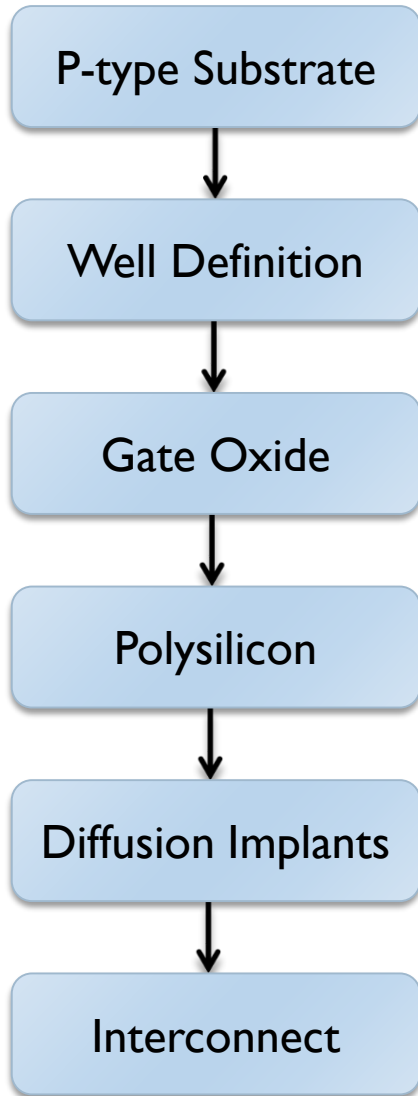
Semiconductors

VLSI Fabrication Process

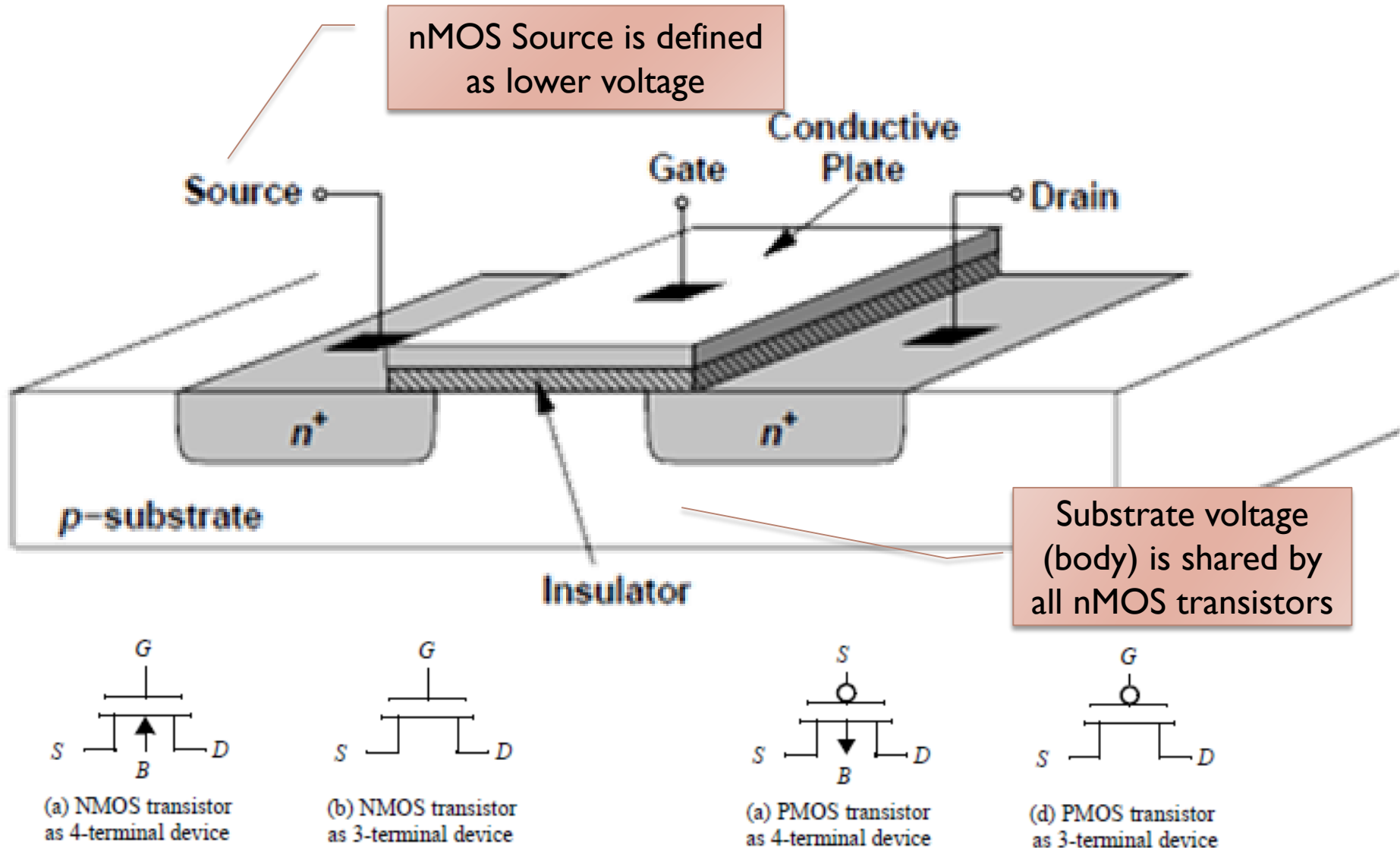
VLSI – Very Large Scale Integration

- ▶ The ability to fabricate many devices on a single substrate within a given process flow/timeframe – independent of the number of devices fabricated.
- ▶ One of the most important inventions of the 20th Century.
- ▶ Similar to a printing press.

VLSI – Transistor Fabrication

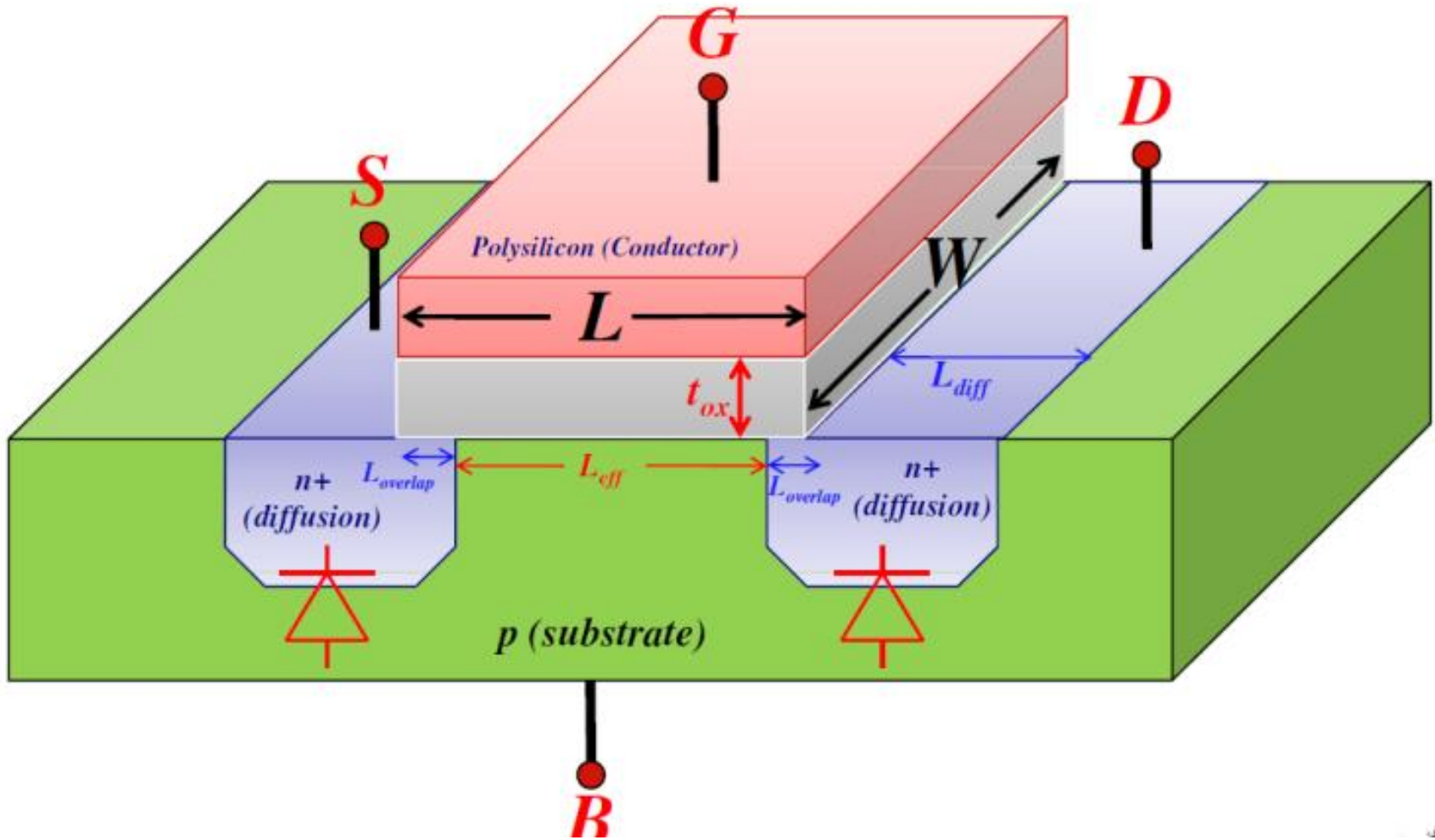


VLSI – nMOS Transistor



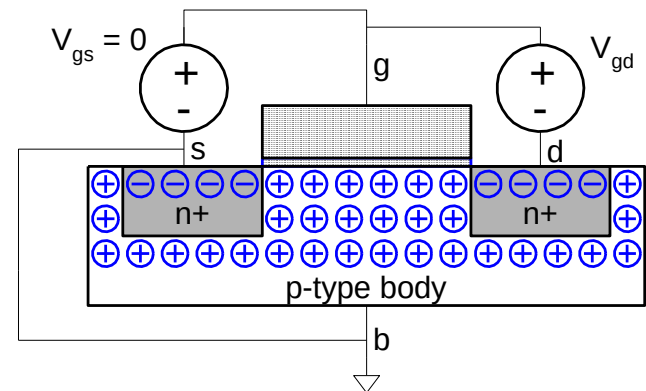
MOS Operation

MOS Operation – Terminals and Sizes



MOS Operation – Cut Off

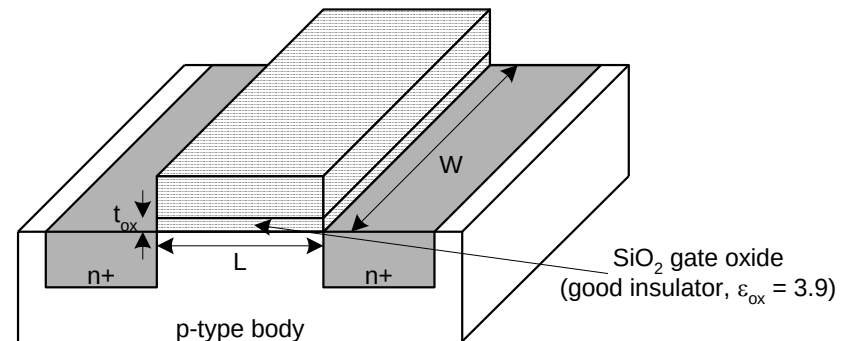
- ▶ $V_{GS} < V_T$
 - ▶ The channel is not Inverted.
- ▶ $I_{DS} = 0$



MOS Operation – Linear Region

- ▶ $V_{GS} > V_T$
 - ▶ The channel is Inverted.
- ▶ $V_{DS} > 0$
 - ▶ The channel has an equivalent resistance.
 - ▶ The current is approximately V_{DS}/R_{eq} .
- ▶ But how is this estimated?
 - ▶ We can integrate the charge over the channel, because:

$$I = Q \cdot v$$



MOS Operation – Linear Region

► **Charge Density:** $\frac{Q(x)}{dx} = \frac{C(x) \cdot V(x)}{dx}$

$$C(x) \approx C_{pp-ox} = \frac{\epsilon_{ox}}{t_{ox}} \cdot W \cdot dx = C_{ox} W dx$$

$$V_{cap}(x) = V_{GS} - V_{XS} - V_T = V_{GS} - V(x) - V_T$$

$$\frac{Q(x)}{dx} = \frac{C_{ox} W (V_{GS} - V(x) - V_T) dx}{dx}$$

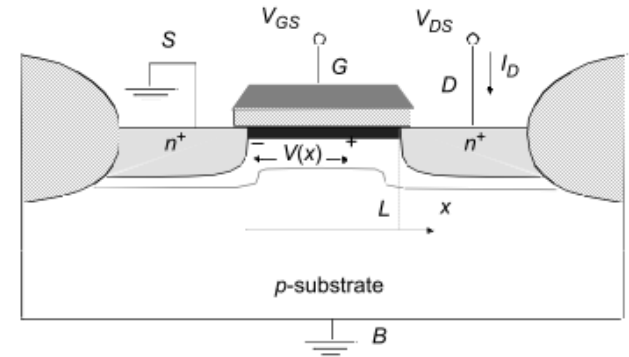
► **Velocity:**

$$v(x) = \mu \cdot \xi(x) = \mu \cdot \frac{dV(x)}{dx}$$

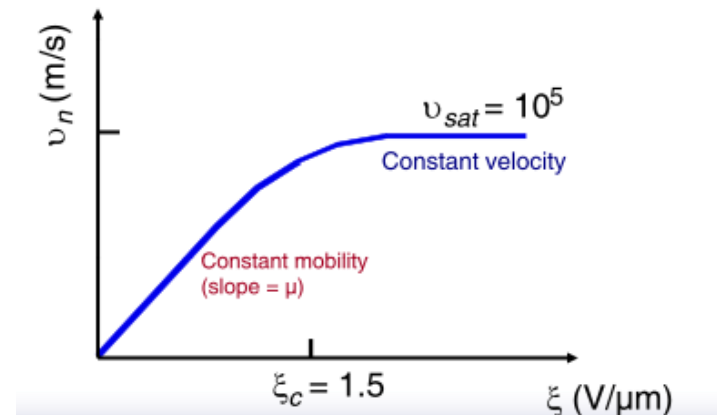
► **Current estimation:**

$$I(x) = Q(x) \cdot v(x) = C_{ox} W (V_{GS} - V(x) - V_T) \cdot \mu \frac{dV(x)}{dx}$$

$$C_{pp} = \frac{\epsilon \cdot A}{l}$$



$$v \left[\frac{m}{\text{sec}} \right] = \xi \left[\frac{V}{m} \right] \cdot \mu \left[\frac{m^2}{V \cdot \text{sec}} \right]$$



MOS Operation – Linear Region

- Integrate the total current in the channel:

$$\int_{x=S}^{x=D} I(x) dx = \int_{V=V_S}^{V=V_D} C_{ox} W (V_{GS} - V(x) - V_T) \cdot \mu dV(x)$$

$$I_{DS} \cdot L = \mu C_{ox} W \left[(V_{GS} - V_T) V_{DS} - \frac{V_{DS}^2}{2} \right]$$

$$I_{DS} = K \left[V_{GT} V_{DS} - \frac{V_{DS}^2}{2} \right]$$

$$K \triangleq \mu C_{ox} \frac{W}{L}$$

MOS Operation – Saturation Region

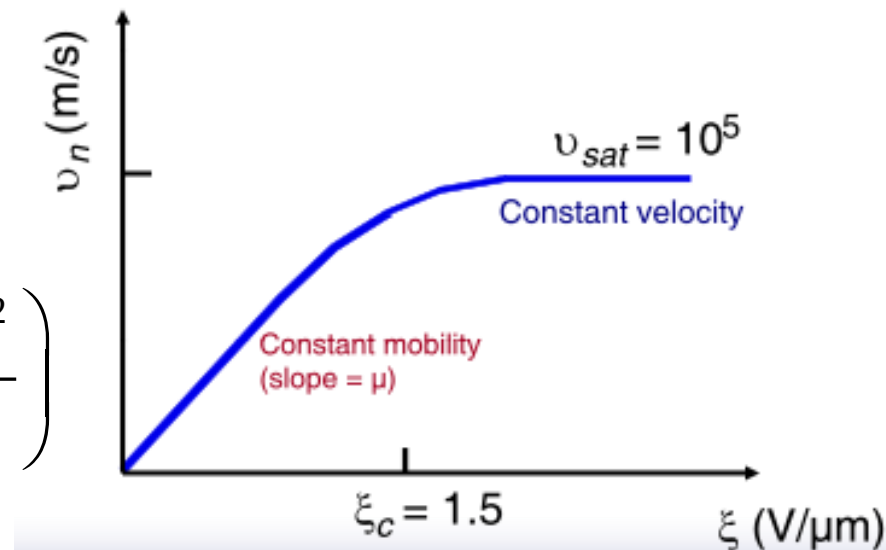
- ▶ $V_{GS} > V_T$
 - ▶ The channel is Inverted.
- ▶ $V_{DS} > V_{GS} - V_T$
 - ▶ The channel is *pinched off*.
 - ▶ The voltage drop over the channel is constant ($V_{GS} - V_T$).
 - ▶ The channel resistance is almost constant.
 - ▶ Therefore the current is almost constant.

$$I_{DS} = \frac{K_N}{2} (V_{GS} - V_{Tn})^2$$

MOS Operation – Velocity Saturation

- ▶ $V_{GS} > V_T$
 - ▶ The channel is Inverted.
- ▶ For a high electric field, the mobility becomes saturated.
 - ▶ We will call the V_{DS} at which this happens “ V_{DSAT} ”
 - ▶ Increasing V_{DS} past V_{DSAT} will not increase the current.

$$I_{DS} = K_N \left((V_{GS} - V_{Tn}) V_{DSATn} - \frac{V_{DSATn}^2}{2} \right)$$



MOS Operation – Channel Length Modulation

- ▶ Is the resistance truly constant as V_{DS} increases?
 - ▶ No, it gets smaller.
 - ▶ The depletion region of the Drain “digs in” to the channel.
 - ▶ The *effective length* is reduced.
- ▶ We call this effect “Channel Length Modulation”
 - ▶ This is almost linearly dependent on V_{DS} .
 - ▶ We will characterize this effect with a coefficient: λ

$$I_{DS} (CLM) = I_{DS} (1 + \lambda V_{DS})$$

□ *During linear operation, this effect is almost negligible...*

MOS Operation – Summary

$$V_{DS,eff} = \min(V_{DS}, V_{DSAT}, V_{GT})$$

$$V_{GT} \triangleq V_{GS} - V_T$$

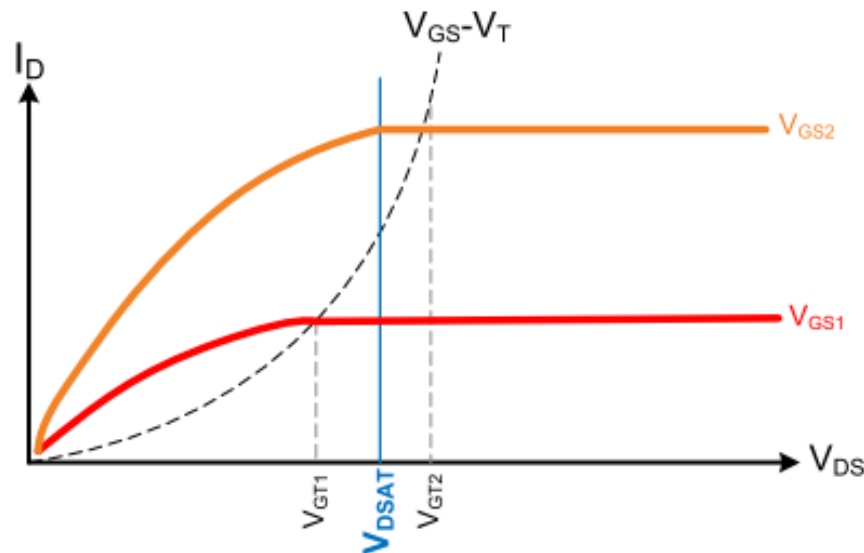
$$K_N \triangleq \mu_N C_{ox} \frac{W_N}{L_N}$$

$$I_{DS} = K_N \left(V_{GT} V_{DS,eff} - \frac{V_{DS,eff}^2}{2} \right) (1 + \lambda V_{DS})$$

Examples

Trick Question: Moed Aleph 2009-10

מהנדס פיתוח בחברת "טרנזיסטור" בע"מ החליט לייעל את המעגלים הדיגיטליים שתוכננו בחברה. לשם כך המהנדס החליט לנצל את תכונות הטרנזיסטור NMOS בצורה טובה יותר. המהנדס התבונן באופיין I_{DS} של הטרנזיסטור, אשר נתון באיור הבא:



להפתעתו המהנדס גילה שהמעגלים שתוכנו בחברה מנצלים רק את תכונות הטרנזיסטור כאשר V_{DS} הינו חיובי ומתעלמים לחלוטם מהערכים השליליים של V_{DS} . עליך לצייר בצורה איכותית את התנהגות הזרם I_{DS} עבור מתחים שליליים של V_{DS} . יש להסביר בקצרה.

Example: Linear vs. Saturation

- ▶ Consider a process with:

$$L_{\min} = 0.4\mu\text{m} \quad t_{\text{ox}} = 8\text{nm} \quad \mu_n = 450 \frac{\text{cm}^2}{\text{V} \cdot \text{s}} \quad V_T = 0.7\text{V} \quad \lambda \approx 0 \quad \epsilon_{\text{ox}} = 3.45 \cdot 10^{-11}$$

- ▶ For a *long channel transistor* with $\frac{W_N}{L_N} = 8\mu\text{m} / 0.8\mu\text{m}$:
 - ▶ Bias the transistor as a current source with of **100μA**.

- ▶ First we will calculate the Transconductance:

$$C_{\text{ox}} = \frac{\epsilon_{\text{ox}}}{t_{\text{ox}}} = \frac{3.45 \cdot 10^{-11}}{8 \cdot 10^{-9}} = 4.32 \cdot 10^{-3} \frac{\text{F}}{\text{m}^2} = 4.32 \frac{\text{fF}}{\mu\text{m}^2}$$

$$k_n' = \mu_n C_{\text{ox}} = 450 \frac{\text{cm}^2}{\text{V} \cdot \text{s}} \cdot 4.32 \frac{\text{fF}}{\mu\text{m}^2} = 1.94 \cdot 10^{-6} \frac{\text{F}}{\text{V} \cdot \text{s}} = 194 \frac{\mu\text{A}}{\text{V}^2}$$

$$k_n = k_n' \frac{W_N}{L_N} = 194 \frac{\mu\text{A}}{\text{V}^2} \cdot \frac{8\mu\text{m}}{0.8\mu\text{m}} = 1.94\text{mA} \frac{\text{A}}{\text{V}^2}$$

Example: Linear vs. Saturation

- ▶ To use our nMOS as a current source, we need to bias it in the Saturation region:

$$I_{DS} = \frac{K_N}{2} (V_{GS} - V_{Tn})^2 = 100 \mu A$$

$$V_{GS} = 1.02V$$

- ▶ But we still need to make sure we are in saturation, so:

$$V_{DS} > V_{GS} - V_T = 0.32V$$

Example: Linear vs. Saturation

- ▶ Now use the device as a resistor with **$R=1k\Omega$** .
- ▶ We now want to operate our transistor in the linear region with a very small V_{DS} .

$$I_{DS} = K_N \left[V_{GT} V_{DS} - \frac{V_{DS}^2}{2} \right] \approx K_N V_{GT} V_{DS}$$

$$R_{eq} = \frac{V_{DS}}{I_{DS}} \approx \frac{V_{DS}}{K_N V_{GT} V_{DS}} = \frac{1}{K_N V_{GT}} = 1000\Omega$$

$$1000 = \frac{1}{194 \cdot 10^{-6} \cdot 10 (V_{GS} - 0.7)} \longrightarrow V_{GS} - 0.7 = 0.52V \longrightarrow V_{GS} = 1.22V$$

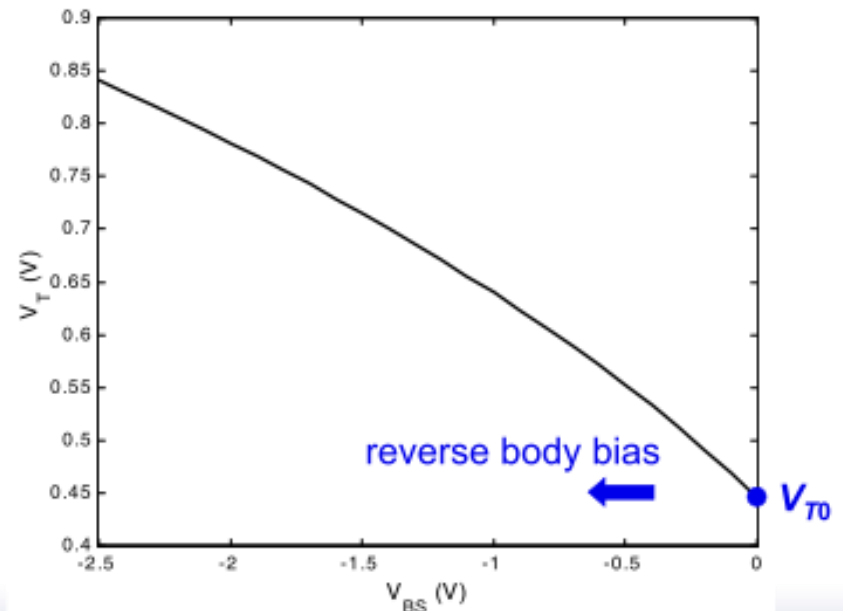
The Body Effect

The Body Effect - Introduction

- ▶ The threshold voltage (V_T) of a transistor is affected by a non-zero potential between the *Source* and *Body*:

$$V_T = V_{T0} + \gamma \left(\left(\sqrt{-2\Phi_F + V_{SB}} \right) - \left(\sqrt{-2\Phi_F} \right) \right)$$

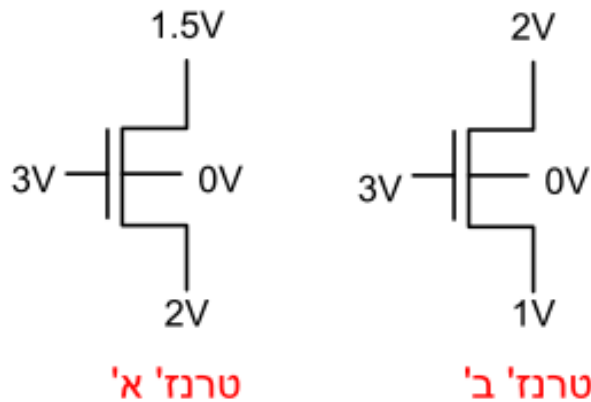
	nMOS	pMOS
Φ_F	-	+
γ	+	-
V_{SB}	+	-



The Body Effect - Example

► Moed Aleph, Semester B, 2008-9

4.2 (4) שני טרנזיסטורי NMOS חוברו כפי שמתואר באיור הבא:



יש לסמן את התשובה הנכונה:

- א. מתח הסף (V_{TH}) של טרנזיסטור א' שווה לזה של טרנזיסטור ב'.
- ב. מתח הסף (V_{TH}) של טרנזיסטור א' גדול מזה של טרנזיסטור ב'.
- ג. מתח הסף (V_{TH}) של טרנזיסטור א' קטן מזה של טרנזיסטור ב'.
- ד. אין מספיק נתונים על מנת לענות על השאלה.

The Body Effect - Example

- ▶ The threshold voltage of a pMOS was measured at standard conditions to be $V_{Tp}(V_{BS}=0)=-0.4V$.
- ▶ Given a body effect coefficient of -0.4 and Fermi Potential of 0.3V, calculate the threshold voltage with a Reverse Body Bias of 2.5V.

$$\begin{aligned} V_T &= V_{T0} + \gamma \left(\left(\sqrt{|-2\Phi_F + V_{SB}|} \right) - \left(\sqrt{|-2\Phi_F|} \right) \right) \\ &= (-0.4) - (0.4) \left(\left(\sqrt{|-0.6 - 2.5|} \right) - \left(\sqrt{|-0.6|} \right) \right) \\ &= -0.4 - 0.4 \cdot 0.98 = -0.79V \end{aligned}$$