

Practice 1:

Logistics, RC Networks, Thevenin-Norton

Course Logistics

Logistics – Times and Location

- ▶ All practice sessions are on Mondays
 - ▶ 1400-1500 – 34/109
 - ▶ 1500-1600 – 28/303
 - ▶ 1600-1700 – 28/107
- ▶ The third session will be recoded and uploaded to the course website for later viewing.
- ▶ Office Hours:
 - ▶ Monday – 1300-1400 (VLSI Center, building 95)

Logistics – Grades and Homework

- ▶ Grade composition:

- ▶ Test – 100%
- ▶ Optional test bonus will be given to those who turn in all homework assignments.

- ▶ Homework:

- ▶ Several homework assignments will be designated as “tasks” on the course website (highlearn).
- ▶ Every student is required to submit *ALL* homework assignments within 2 weeks of publication to be eligible for bonus.
- ▶ **Submission is via highlearn!** Homework may be done in pairs, but submission has to be individual.

Logistics – Final Exam

- ▶ The test will be closed book.
- ▶ A formula sheet will be attached to the test. An example sheet will be published on the course website.
- ▶ The test will include all the course material that will be covered in the lectures, practices, and homework.
- ▶ Many examples of former tests are available and you are advised to use them to prepare for the test.
- ▶ The three tests will be at the same (*high!*) level. They will have **different** questions about **different parts** of the material.

Logistics – Course Website

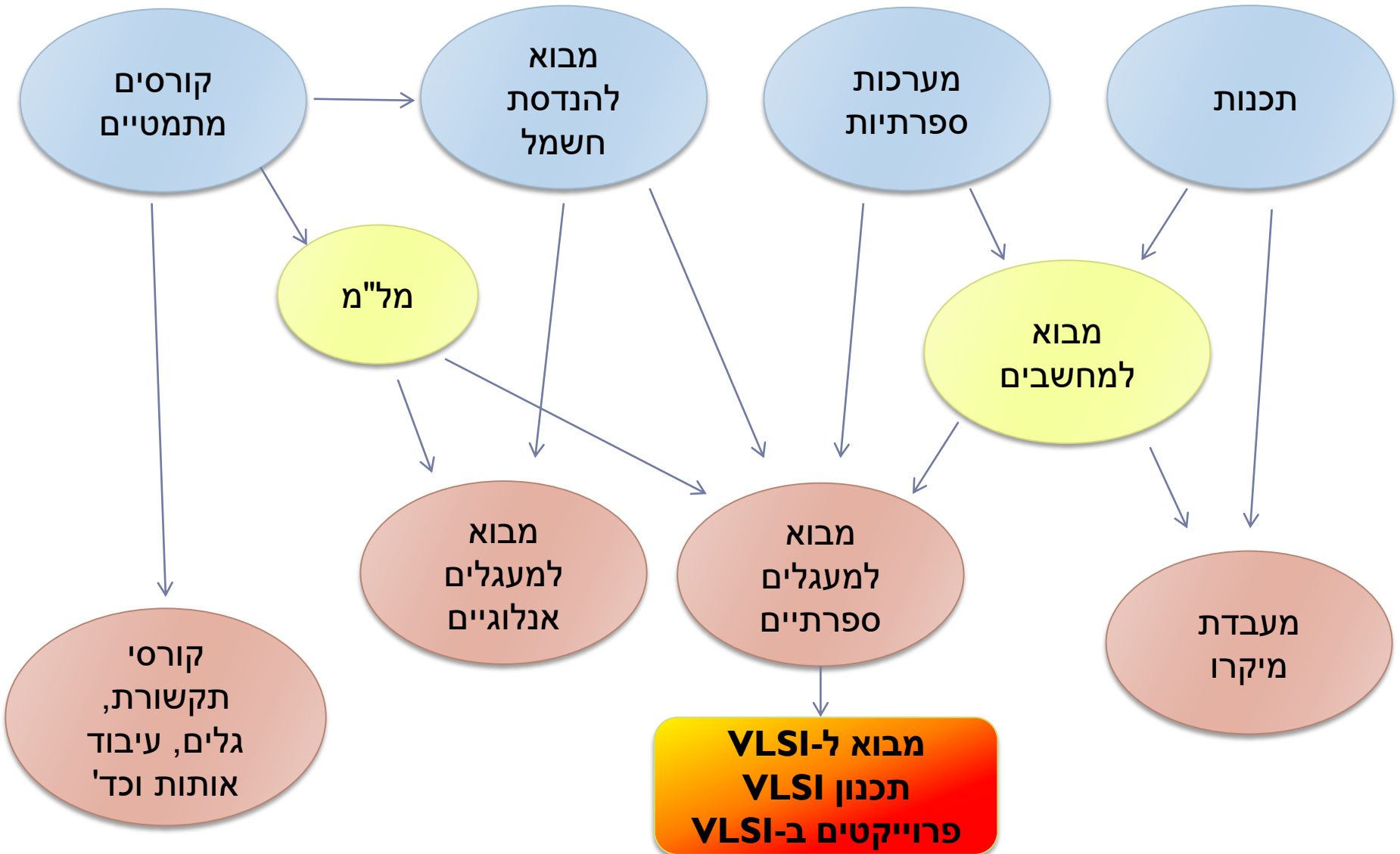
- ▶ The course website is ***highlearn***.
- ▶ All course content and discussion will be through the website:
 - ▶ **Lectures** – 4 slide per page *pdf* files will be uploaded weekly.
 - ▶ **Practices** – Full explanations and solutions in a *pdf* document will be uploaded weekly.
 - ▶ **Practices (2)** – Presentations used during practice sessions will be uploaded. (*ppt*) Following the practice session, annotated slides will be uploaded.
 - ▶ **Homework** – Will be published and submitted through the website.
 - ▶ **Discussion Forum** – Questions can be asked in the forum. If not answered by other students, we will try and answer them.
- ▶ Questions via direct emails to Dr. Fish or me will not be answered!

Logistics - Bibliography

- ▶ Rabaey, et al.:
 - ▶ Digital Electronic Circuits: A Design Perspective – 2nd Edition
- ▶ Sedra & Smith
 - ▶ Microelectronic Circuits
- ▶ Weste & Harris
 - ▶ CMOS VLSI Design: A Circuits and Systems Perspective

Short Introduction

Introduction – Where Are We?



Introduction – Digital? Analog? Us?

First Order RC Circuits

RC Circuits - Motivation

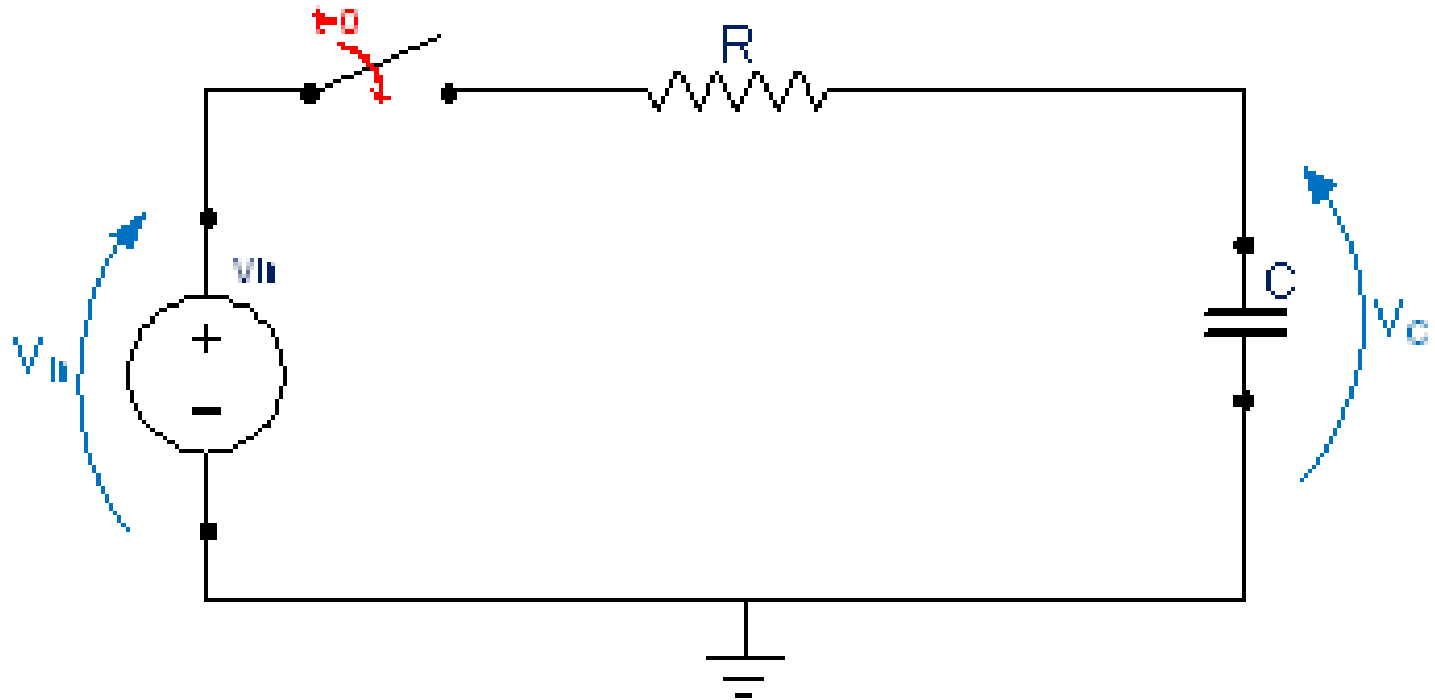
RC Circuits - Example

► Given:

- R, C, V_{in}
- $V_c(0) = V_0$
- The switch closes at $t=0$.

► Find:

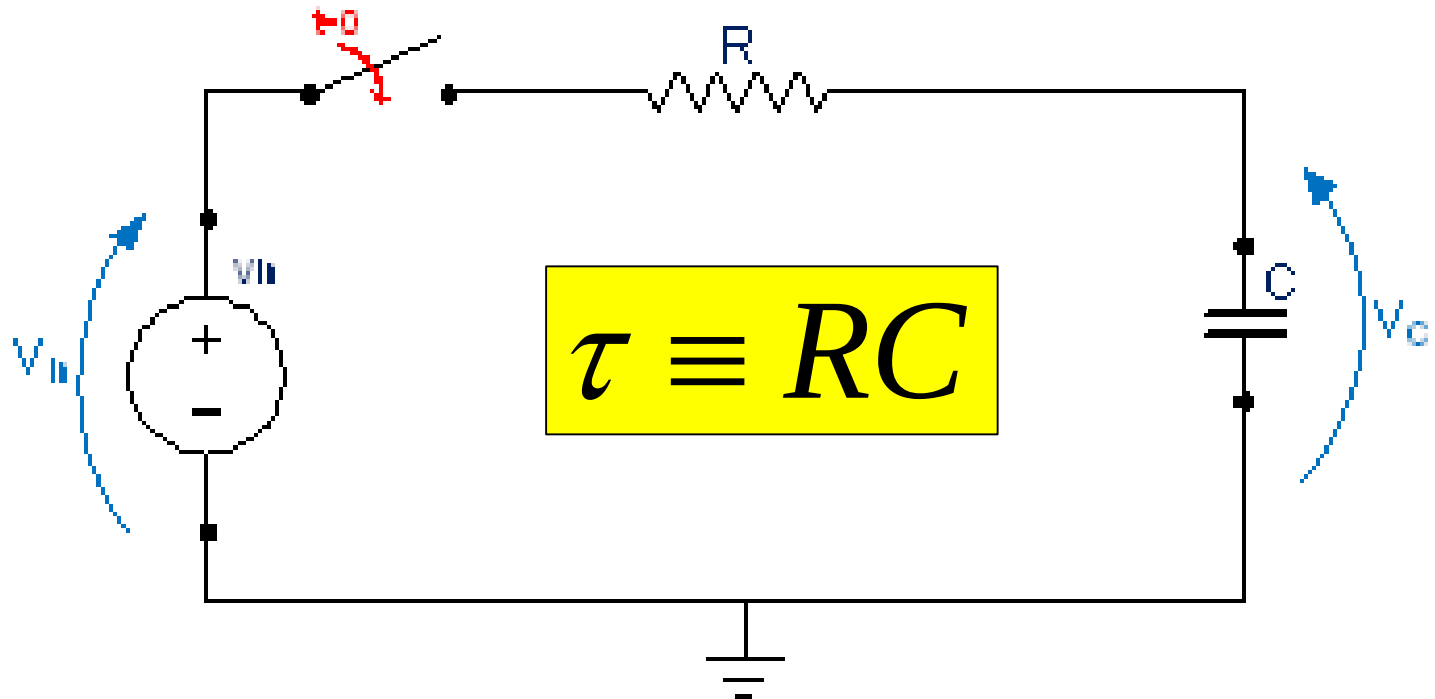
- $V_c(t)$



RC Circuits - Example

► KVL: $V_{in}(t) = V_c(t) + V_R(t) = V_c(t) + i_C(t)R$

$$V_{in} = V_c + RC\dot{V}_c = \tau\dot{V}_c + V_c$$



RC Circuits - Example

- ▶ First Order Differential Equation:

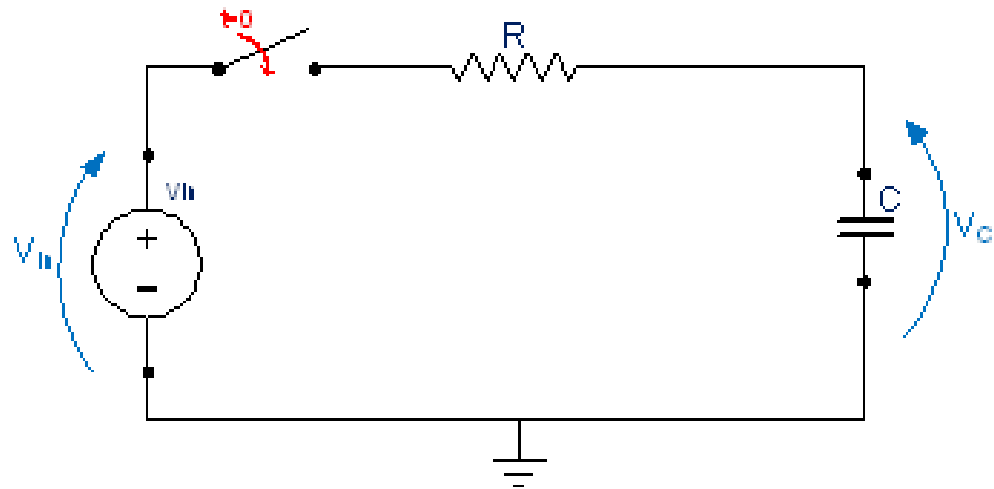
$$V_{in} = V_c + RC \dot{V}_c = \tau \dot{V}_c + V_c \quad \longrightarrow \quad V_c(t) = V_{ch}(t) + V_{cp}(t)$$

- ▶ Homogeneous Solution:

$$V_{ch}(t) = K e^{-t/\tau}$$

- ▶ Particular Solution:

$$V_{cp}(t) = V_{in}$$



RC Circuits - Example

► General Solution:

$$V_c(t) = V_{ch} + V_{cp} = Ke^{-t/\tau} + V_{in}$$

$$V_c(0) = V_0 = Ke^{-0/\tau} + V_{in} = K + V_{in}$$



$$K = V_0 - V_{in}$$

$$V_c(t) = (V_0 - V_{in})e^{-t/RC} + V_{in}$$

$$= V_0 e^{-t/RC} + \left(1 - e^{-t/RC}\right) V_{in}$$

RC Circuits – Using this solution

- How long will it take to charge the capacitor to $V_{in}/2$?

$$V_c(t) = (V_0 - V_{in})e^{-t/RC} + V_{in}$$

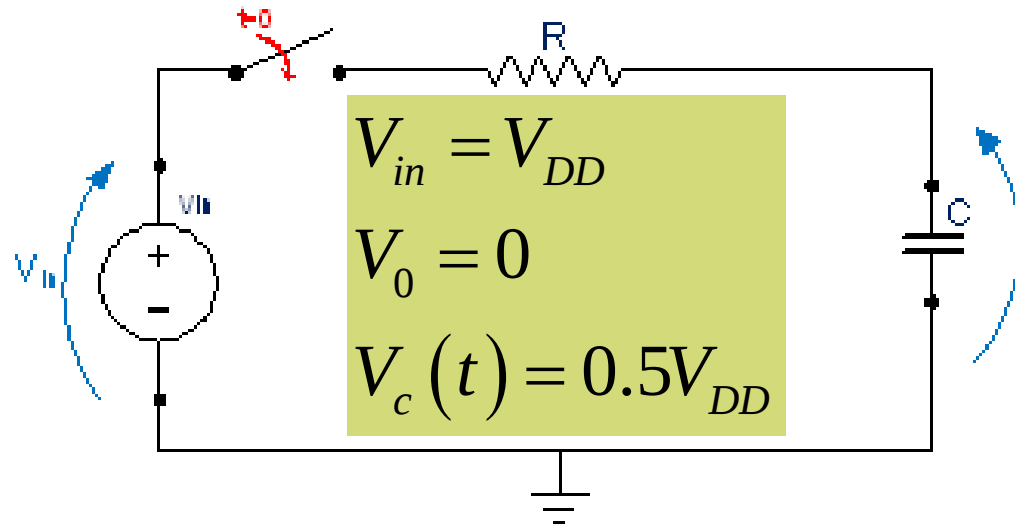
$$e^{-t/RC} = \frac{V_c - V_{in}}{V_0 - V_{in}}$$



$$t = RC \ln \frac{V_0 - V_{in}}{V_c - V_{in}} \equiv \tau \ln \frac{V_c(0) - V_c(\infty)}{V_c(t) - V_c(\infty)}$$

$$t = RC \ln \frac{-V_{DD}}{0.5V_{DD} - V_{DD}} = RC \ln 2$$

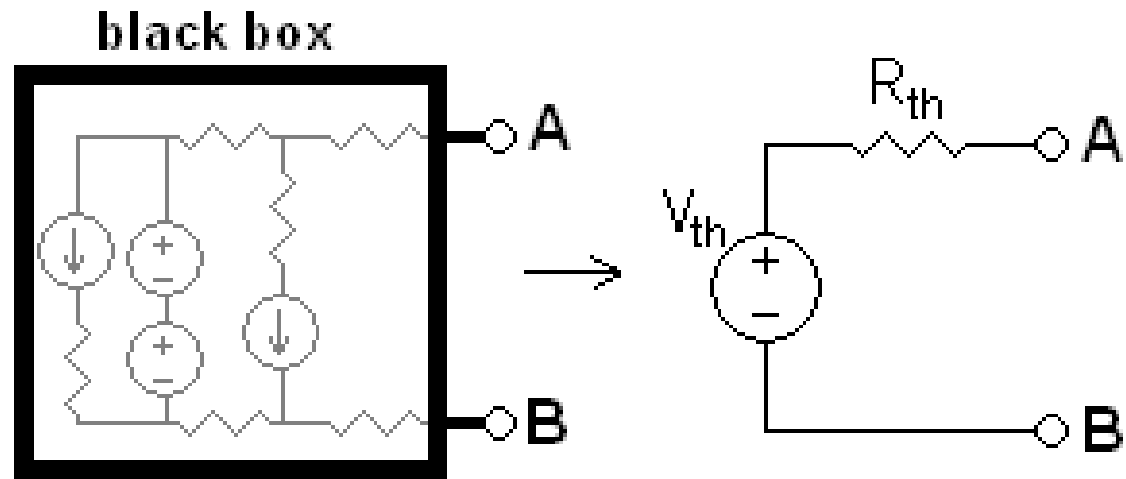
$$t = 0.69\tau$$



Thevenin-Norton Equivalents

Thevenin - Norton – A reminder...

- ▶ Remember that in Introduction to Electrical Engineering you learned *Thevenin's Theorem*?
- ▶ Any linear circuit – no matter how complex – can be simplified into a Voltage Source and Equivalent Impedance driving a load.
- ▶ By using a Thevenin Equivalent circuit, we *don't care* what's going on inside the circuit. This simplifies the equations drastically.



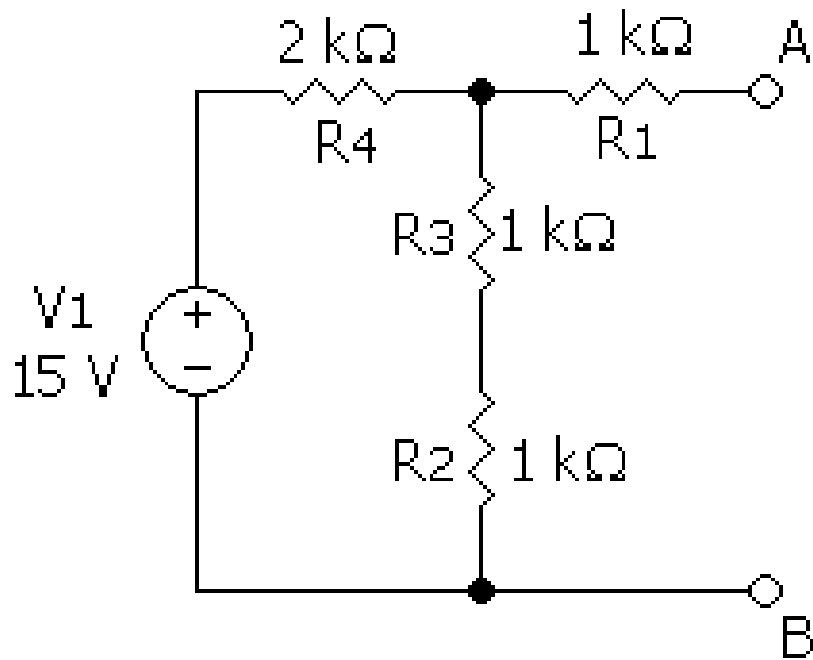
Thevenin – Calculation Method

- ▶ 1. Find the *Open Circuit Voltage* (V_{OC}):
 - ▶ Disconnect the *Load*.
 - ▶ Find the Voltage between the terminals of the load.

- ▶ 2. Find the *Short Circuit Current* (I_{SC}):
 - ▶ Short circuit the *Load*.
 - ▶ Find the Current between the load terminals.

- ▶ 3. Calculate the Thevenin Equivalent Voltage and Impedance:
 - ▶ $V_{Thevenin} = V_{OC}$
 - ▶ $R_{Thevenin} = V_{OC} / I_{SC}$

Thevenin – Example

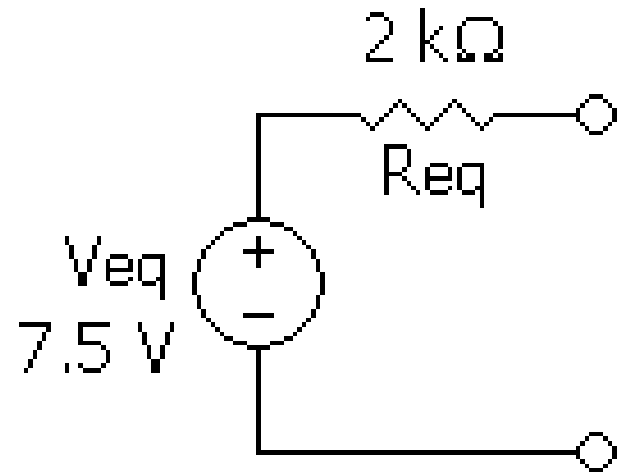


$$V_{Thevenin} = 7.5V \quad R_{Thevenin} = 2k\Omega$$

$$V_{OC} = V_{in} \frac{R_3 + R_2}{R_4 + R_3 + R_2} = 7.5V$$

$$I_{SC} : KCL \rightarrow \frac{15 - V_x}{2k} = \frac{V_x}{1k} + \frac{V_x}{2k} \quad I_{SC} = \frac{V_x}{1k}$$

$$15 - V_x = 3V_x \quad V_x = 15/4 \quad I_{SC} = 15/4k$$



Norton – Reminder

- ▶ Norton equivalent circuits are the same as Thevenin Equivalents, but they incorporate a current source instead.
- ▶ To find the Norton Equivalent:
 - ▶ 1. The Norton Resistance is the same as the Thevenin Resistance.
 - ▶ 2. The Norton Current Source is the Short Circuit Current.

